

## Chapter → Thermodynamics and Thermochemistry

**System** → Part of Total universe  
for which energy changes  
are discussed

represent  
Matter (s, l, g)  
Under study

Amount  
fixed  
(mass, moles)

**Surrounding** → Part of universe around  
System is called surrounding.

**Boundary (B)** → Region which separates  
System & Surrounding

B → • can be real or Imaginary  
• flexible or Rigid  
• conducting or Insulator (electrical) (Heat exchange possible)  
• Thermally conducting or (Diathermic)  
Thermally insulator (Adiabatic Boundary)  
no heat exchange b/w  
System & surrounding

## # Depending upon Boundary type of system

open → Matter exchange ✓  
Heat exchange ✓

closed → Matter exchange ✗  
Heat exchange ✓

Isolated → Matter exchange ✗  
Heat exchange ✗

No connection  
with surrounding

Boundary is  
adiabatic

## # Property of system

→ applicable for bulk of system / Macroscopic Nature  
& not for a single particle (Microscopic nature)

→ Value of property is defined / obtained at Thermodynamic Eq<sup>n</sup> state (cond<sup>n</sup>)

At Equilibrium,  
state change is  
opposed without  
any external effect  
*Spiral*

Total Bulk is defined  
by single value of any  
property.



# # Properties of system or properties of matter in system.

## 1) Intensive

- Properties which are independent of amount / mass of substance in system.

→ If we cut (System) or matter into 2 equal Halves, value of property does not change.

eg<sup>n</sup> elasticity, Refractive index, density, <sup>gas</sup> Pressure, Temperature, molarity, Normality, electrode Potential, conductivity, Resistivity, molar heat capacity, specific heat capacity, molar Entropy, Molar Internal Energy ( $U$  or  $E$ ), molar Mass ( $M$ ), Gibbs free Energy ( $G$ ), molar Enthalpy ( $H$ ) etc.

## 2) Extensive (or Extrinsic)

→ Those properties whose value depend on amount of substance in system.

→ Cutting the system in two equal Halves, value of property becomes half for each half of substance system.

eg<sup>n</sup> → mass, volume, Heat capacity ( $C$ ), moles,  $C_p$ ,  $S$ ,  $H$ , etc.

#  $\text{Ext} = \text{Intensive}$   
 $\text{Ext}$

$U \rightarrow \text{Ext}$   
 mole  $\rightarrow \text{Ext}$  = molar Internal Energy ( $U_n$  or  $U_m$ )  
 $\rightarrow \text{Int.}$

$m \rightarrow \text{Ext}$   
 $V \rightarrow \text{Ext}$  = density (Int.)

#  $\text{Ext} \times \text{Ext} \neq \text{Int.}$

# density =  $\frac{\text{mass}}{\text{volume}}$

#  $\text{Ext} - \text{Ext} \neq \text{Int.}$

# specific =  $\frac{\text{Volume}}{\text{mass}}$  -  $\frac{1}{\text{dens.}}$   
 $\downarrow$   
 Int.

## Thermodynamic state of system

→ at thermodynamic Eq<sup>n</sup>, A state (condition) of Substance (Matter) in system specified by certain measurable macroscopic properties.  
 (Int. or Ext.)

→ properties can be T, P, density, volume etc

# Value of properties for a particular state remains fixed until thermodynamic Eq<sup>n</sup> of system is maintained.



- ① When state of system changes from one eq<sup>n</sup> point to another eq<sup>n</sup> point; value of properties at those states also changes & those properties at those states which are dependent only on the present state (irrespective of path taken to reach the state) are called state variables or functions or properties.

- ② change in state function or variable  
↓  
depend only on initial and final state.

$$\Delta T = T_2 - T_1$$

↓  
change in state function

③ Reversible expansion/  
compression work → state  
function

T → state function or variable

- ④ T, P, V etc → state variable / property

If (T) is obtained from values of P & V (independent variables) for any state then Temp. becomes variable state function for that state.

- ⑤ Path function → Function which depends on path taken to reach from one state of system to another state of system. eg<sup>n</sup> → Work, Heat, Heat capacity

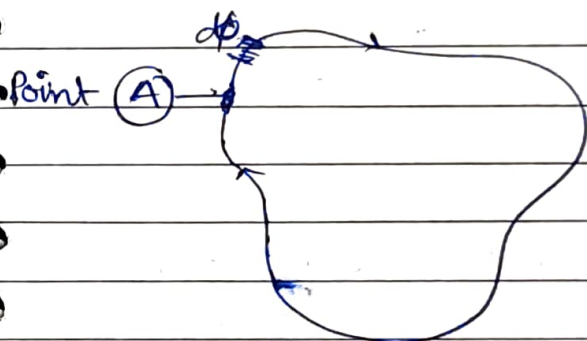
# (#) Conditions for function to become state function

(1) Cyclic Integration is zero

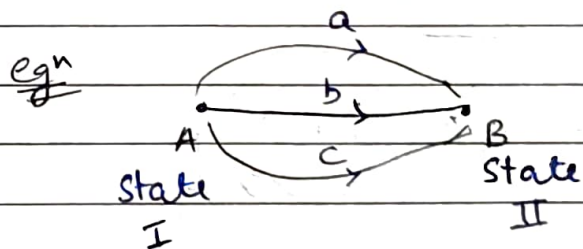
$$\text{Initial state} = \text{final state}$$

let  $\phi$  is a function

$$\oint_A^A d\phi \text{ or } \oint d\phi = 0, \text{ then } \phi \text{ is a state function}$$



(2) B/w 2 states, change in state function is same for all the path taken



let  $\phi$  is a function

for  $\phi$  to be state function

$$(\Delta\phi)_a = (\Delta\phi)_b = (\Delta\phi)_c$$



③ Euler's reciprocity theorem must be satisfied

let  $\phi$  is function of  $x$  &  $y \Rightarrow \phi = f(x, y)$   
~~for  $\phi$  to be state fun<sup>n</sup>~~

$$\left[ \frac{\partial}{\partial x} \left( \frac{\partial \phi}{\partial y} \right)_x \right]_y = \left[ \frac{\partial}{\partial y} \left( \frac{\partial \phi}{\partial x} \right)_y \right]_x$$

or

$$\left[ \frac{\partial^2 \phi}{\partial x \partial y} \right]_{x, y}$$

①  $\rightarrow$  Prove Pressure of 1 mole ideal Gas is state function.

Sol<sup>n</sup>

$$PV = RT$$

$$P = f(V, T)$$

$$P = \frac{RT}{V}$$

$$\text{To prove: } \left[ \frac{\partial}{\partial T} \left( \frac{\partial P}{\partial V} \right)_T \right]_V = \left( \frac{\partial}{\partial V} \left( \frac{\partial P}{\partial T} \right)_V \right)_T$$

$$-\frac{R}{V^2}$$

$$-\frac{R}{V^2}$$

Hence Proved.

No change in  
Date ... Pressure or  
Process per unit time

(#) Thermodynamic  $eq^n$   $\rightarrow$  Mechanical  $eq^n$   
(No pressure gradient)

Chemical  $eq^n$  Thermal  $eq^n$   
(No temp. gradient)

In Reversible  $Rx^n$  :-

No concentration gradient for  
any species in  $Rx^n$

$\hookrightarrow$  conc. of every species  
becomes const. (does not  
change with time) when  
 $eq^n$  is achieved

at this cond<sup>n</sup> only  
we can find  
value of any  
macroscopic  
property in  
any state of  
system.

(#) Thermodynamic process :- Any method / process  
by which system can  
change its state from one state  
of thermodynamic  $eq^n$  to another  
thermodynamic  $eq^n$ .

(\*\*) During the process, value of any macroscopic  
property cannot be defined.

(\*\*) If process occurs keeping any state property  
const., then iso prefix is used.

$\rightarrow$  Process occurs at const. Temp ; Isothermal  
Process  
 $T = \text{const.}$   
 $\Delta T = 0$

Spiral

Small  $\left( \frac{dT}{dt} \right) = 0$   
change in Temp.



→ Process occurs at const vol; Isochoric Process  $\Delta V = 0$   
 $dV = 0$

→ " " " " Pres. Isobaric Process  $dP=0$   
 $\Delta P=0$

→ Adiabatic process → No heat exchange b/w system & Surrounding during the process.

$q \text{ or } q = 0$

→ Cyclic Process → Initial state = final state

change in state funct = 0

Work done or heat exchange  $\neq 0$

## Classification of thermodynamic processes on the Basis of the way these processes are carried out :-

### ① Reversible Process

If a process is carried out in such a manner, so that the system is always in thermodynamic eq<sup>n</sup> at every stage of the process.

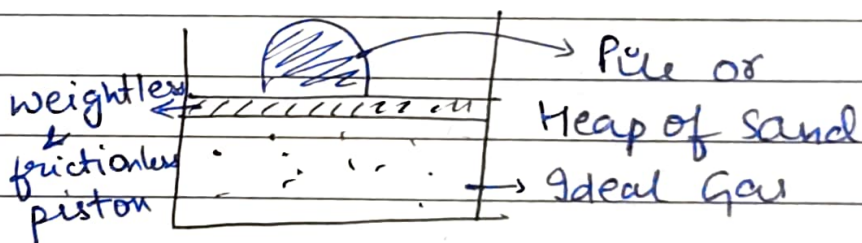


If the process is carried out such that the difference is driving force and opposing is infinitesimally small. So, that process takes place at infinitesimally slow rate.  
 $\hookrightarrow$  negligibly

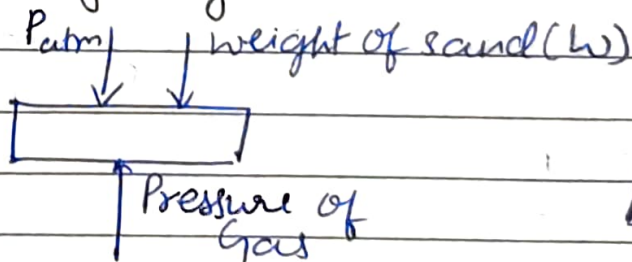
$$F_{\text{driving}} = F_{\text{opposing}} \pm df \quad \boxed{df \rightarrow 0}$$

① An ideal Reversible Process will take infinite time for completion  $\rightarrow$  reaching from initial state to required final state.

② Let's consider an example  $\div$



Initially system at Rest (Eq<sup>n</sup>)



$$P_{\text{atm}} + \frac{W}{A} = P_g$$

$\hookrightarrow$  Area



- If one sand particle is removed such that  $eq^n$  is not disturbed b/w system & surrounding.

piston moves upwards giving infinitesimally small volume change due to small diff in opposing Pressure ( $P_{ext}$ ) and (External)

Pressure of Gas  
(driving force)

for negligible expansion of Gas

$$P_{ext} = (P_{int}) - dP \quad dP \rightarrow 0$$

$P_g$

↳ very small step of expansion

- \*\*\* If one sand particle is kept on piston, very small compression is observed.

$$P_{ext} = P_g + dP \quad (dP \rightarrow 0)$$

So, for Reversible process at every small step

$$P_{ext} = P_g \pm dP$$

## ② Irreversible process :-

If process is carried out in such a manner so that the system is in thermodynamic

equilibrium only at initial and final state of the process.

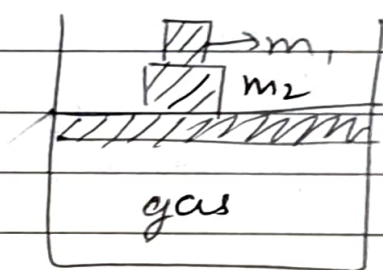
(\*\*) There will be no equilibrium b/w system & surrounding during process.

(\*\*) Steps are Big involving Big change in macroscopic properties.

(\*\*) Irreversible can be completed in finite steps (1, 2, 3, ...)

(\*\*) Diff. b/w opposing force & Driving force is finite.

eg<sup>n</sup>



• If  $m_1$  is removed

$P_{ext}$  (opposing Press) is  $P_{atm} + \frac{m_2 g}{A}$

& gas expands under this Pressure  $\left[ P_{atm} + \frac{m_2 g}{A} \right]$

Initially  $P_g \neq P_{ext}$

So,  $P_{ext}$  remain const.

$P_{atm} + \frac{m_2 g}{A} + \frac{m_2 g}{A}$  during any step of process.

• If  $m_2$  is also removed, gas expands under

$$P_{ext} = P_{atm}$$

$$\text{till } P_g = P_{ext} = P_{atm}$$



★ Heat and Work — Two ways by which system can interact or can exchange energy with its surroundings

Heat ÷ Energy exchange due to temp. diff. b/w syst. & surr.

Work ÷ Energy exchange takes place not due to temp. diff. but due to difference in opposing force & driving force.

Sign Convention

$q = +ve$  (Heat absorbed by system)

$q = -ve$  (Heat released by system)

Chemistry → we are external (surrounding)

System (Expansion of Gas)  
 $W$ . done by system =  $-ve$   
 $W$ . done by surrounding =  $+ve$   
 (Compression)

Physics → we are inside system or we are system.

$W$ . done by system =  $+ve$  (Expansion)  
 $W$ . on system =  $-ve$  (Compression)

# # Internal Energy (E or U)

Sum of all possible ~~value~~ forms of Energy associated with matter in any thermodynamic state of system at given Temp.

Extensive

$$U = K.E + P.E + \dots$$

State function

= Translational K.E + Rotational K.E + Vibrational K.E + Attractive Energy + Repulsive Energies + Bond Energy + ...

\*\* Energy due to External field effect is not considered

↳ gravitational field, magnetic etc.

\*\* Absolute value of U cannot be determined we always find change of U by FLOT. (First law of Thermo.)

for ideal gas,

• No interaction b/w gas molecules P.E.

•  $U = [K.E] \rightarrow$  only dependent of Temp.

• U is function of T only for Ideal Gas.



$$\Delta U = \Delta K.E$$

$$\left(\frac{\partial U}{\partial V}\right)_T = 0 = \left(\frac{\partial U}{\partial P}\right)_T \text{ for ideal Gas}$$

for Real Gas,

$U$  is function of  $(T, P, V)$

$$\left(\frac{\partial U}{\partial V}\right)_{T,P} \neq 0$$

$$\left(\frac{\partial U}{\partial P}\right)_{T,V} \neq 0$$

## Law of equipartition of Energy :-

\* Energy equal to  $\frac{1}{2}kT$  is associated with each degree of freedom per ideal Gas molecule.

D.o.f Degree of freedom  $\rightarrow$  No. of ways in which energy of molecule can be distributed.  
or  
f

Types :-

(i)  $f_T$  (Translational d.o.f)

(ii)  $f_R$  (Rotational d.o.f)

(iii)  $f_V$  (Vibrational d.o.f)

vibrat<sup>n</sup> in Bond occur at High Temp.

$T \approx 500^\circ\text{C}$  or above

$$f_T + f_R + f_V$$

\* Total Dof (f) for any molecule =  $3N$   
No. of atoms in molecule

at Room Temp, only  $f_T + f_R$  exist

$$f_T = 3$$

→ always for every type of gas

a) Monoatomic Gas ÷

$$f_R = 0, f_V = 0, \boxed{f_T = 3} \Rightarrow \text{along } x, y, z$$

eg<sup>n</sup> → He, Ne, ~~Ar~~ etc

$$\rightarrow \text{Total D.o.f} = 3N = 3 \times 1 = 3$$

b) Diatomic Gas ÷

$$\boxed{f_T = 3}$$

$$\boxed{f_R = 2}$$

$$\boxed{f_V = 1}$$

eg<sup>n</sup> → CO, O<sub>2</sub>, Cl<sub>2</sub>, Br<sub>2</sub> etc

$$\rightarrow \text{Total D.o.f} = 3 \times 2 = 6$$

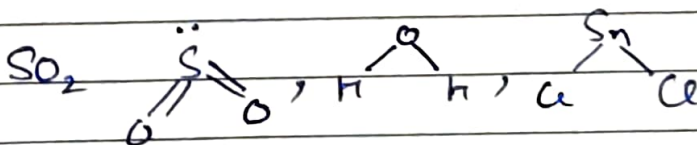
c) Triatomic Gas

→ Triatomic Linear (Like  $\text{O}=\text{C}=\text{O}$ ,  $\text{F}-\text{Xe}-\text{F}$ ) (Diatomic)  
CO<sub>2</sub>, XeF<sub>2</sub>

$$f_T = 3, f_R = 2, f_V = 4$$

↓  
Triatomic Non-Linear

$$f_T = 3, f_R = 3, f_V = 3$$





d) Polyatomic Gas  $\Rightarrow f_T = 3, f_R = 3, f_V = 3N - 6$

$$\text{Total} = 3N$$

for 1 d.o.f,  $\overline{K.E}$  or  $E = \frac{1}{2} kT$  per molecule

$$= \frac{1}{2} RT \text{ per mole}$$

at Room Temp.

for  $f$  dof,  $\overline{K.E} = \frac{f}{2} kT$  per molecule of Gas  
 $\rightarrow f_T + f_R$

$$= \frac{f}{2} kT \text{ per molecule}$$

$f_V \rightarrow$  neglected

$$\Delta \overline{K.E} = \Delta U \quad (\text{for Ideal Gas})$$

$$\boxed{\frac{f}{2} R(\Delta T) = \Delta U} \rightarrow \text{for 1 mole}$$

for n mole of Ideal Gas

$$\boxed{\frac{f}{2} n R \Delta T = \Delta U}$$

$$\boxed{f = f_T + f_R}$$

$$= 3 (\text{mono})$$

$$= 5 (\text{Di or Tri linear})$$

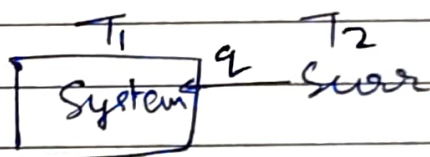
$$= 6 (\text{Tri Non-linear})$$

(#) Heat ( $q$  or  $Q$ )  $\div$   ~~$q$~~

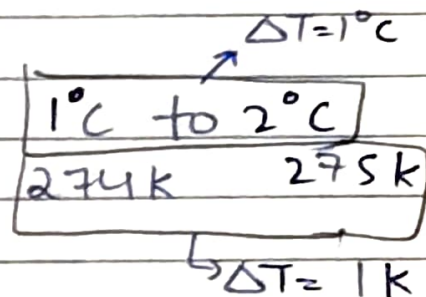
Energy flow or energy exchange b/w System and surrounding due to Temp. difference

System  $\Rightarrow$  Temp. of System  $T$ ed from  $T_1$  to  $T_2$

Heat ( $q$ ) from surrounding to system is transferred due to temp. difference ( $\Delta T = T_2 - T_1$ )



$$T_2 > T_1$$



$$C = \frac{q}{\Delta T} \leftarrow 1^\circ\text{C}$$

Heat capacity of substance in system

Specific Heat capacity ( $s$ )  $\Rightarrow$   $s = \frac{C}{\text{mass}}$

Molar Heat Capacity ( $C_n$ )

$$\frac{C}{m/m} = \frac{C}{\text{mole}(n)} = C_n = \frac{q}{n \times \Delta T}$$



$$\boxed{\frac{M \cdot C}{m} = C_n} = \boxed{M \cdot s} \rightarrow \text{intensive}$$

①

Al  
9g

← 30J

25°C to 31°C

$$C = \frac{30}{6} = 5 \text{ J/K or } 5 \text{ J/}^\circ\text{C}$$

$$s = \frac{5 \text{ J K}^{-1} \text{ gm}^{-1}}{9}$$

$$C_n = \frac{5 \times 9^3}{9} = 15 \text{ J K}^{-1} \text{ mol}^{-1}$$

②

$q \leftarrow \Delta T \text{ (}^\circ\text{C or K)}$

(Heat Capacity)  $C = \frac{q}{\Delta T} \leftarrow 1(^\circ\text{C or K})$

unit = J/K  
or  
J/°C

amount or mass  
dependent  
(Extensive)

## # Specific Heat capacity of substance ( $s$ )

Heat required by substance to change its temp. by  $1^\circ\text{C}$  or  $\text{K}$  for 1 gram substance

$$s = \frac{q}{m\Delta T} = \frac{C}{m} \rightarrow \text{Heat capacity}$$

$\downarrow$   
defined for given mass

$\rightarrow$  mass of substance

$\rightarrow$  Unit  $\rightarrow \text{J}(\text{}^\circ\text{C})^{-1}\text{gm}^{-1}$  or  $\text{JK}^{-1}\text{gm}^{-1}$

## # Molar Heat Capacity ( $C_n$ )

Heat required to change temp. by  $1^\circ\text{C}$  or  $\text{K}$  for 1 mole substance.

$$C_n = \frac{q}{n\Delta T} = \frac{C}{n} = \frac{C}{m} \times M = \frac{C}{m} \times M$$

$\downarrow$   
moles of substance

$\rightarrow \text{JK}^{-1}\text{mol}^{-1}$

$n = \frac{\text{mass}(m)}{\text{Molar mass}(M)}$

## # Total Heat ( $q$ ) exchange

$$= C\Delta T$$

$$= ms\Delta T$$

$$= nC_n\Delta T$$

$\rightarrow$  find Total Heat absorbed by 100 g water when it is heated from  $25^\circ\text{C}$  to  $45^\circ\text{C}$ .  $s(\text{water}) = 4.2 \text{ J}(\text{}^\circ\text{C})^{-1}\text{gm}^{-1}$



Soln

$$q = m \times s \times \Delta T$$

$$q = (100 \times 4.2 \times 20) \text{ J}$$

$$= \frac{100 \times 4.2 \times 20 \text{ cal}}{4.18}$$

$$= \frac{100 \times 4.2 \times 20}{1000} \text{ KJ}$$

① Molar Heat capacity ( $C_m$ ) at

Const. Volume process  $\rightarrow C_{m,v}$  or  $C_v$ .

② Molar heat capacity ( $C_m$ ) at

Const. Pressure process  $\rightarrow C_{m,p}$  or  $C_p$

③ Molar Heat Capacity  $C_m \rightarrow \infty$  (for isothermal)

$$\Rightarrow \Delta T = 0$$

$\rightarrow 0$  (for adiabatic)  $\Rightarrow q = 0$

for Solids/liq  $\rightarrow C_p \approx C_v$

for gases  $\Rightarrow C_v = \frac{q_v}{n\Delta T} \rightarrow$  Heat exchange at const. v

$C_p = \frac{q_p}{n\Delta T} \rightarrow$  Heat exchange at const. P

④ Meyer's Relation

Relation b/w  $C_p$  &  $C_v$

Date .....

$$C_p - C_v = R$$

$$C_p = R + C_v$$

#  $\frac{C_p}{C_v} = \gamma$  (Poisson's Ratio)

$$\gamma > 1$$

$$C_p > C_v$$

#  $C_v = \frac{f}{2} R$

$$C_p = \left( \frac{f+2}{2} \right) R$$

T = Moderate or Room Temp.

Atomicity of Gas

$C_v$

$C_p$

$\gamma$

Mono

$$\frac{3R}{2}$$

$$\frac{5R}{2}$$

$$\frac{5}{3} = 1.67$$

Dia or Tri(L)

$$\frac{5R}{2}$$

$$\frac{7R}{2}$$

$$\frac{7}{5} = 1.40$$

Tri (NL)

$$\frac{6R}{2} = 3R$$

$$\frac{8R}{2} = 4R$$

$$\frac{4}{3} = 1.33$$

Polyatomic

$$3R$$

$$4R$$

$$\frac{4}{3} = 1.33$$

#  $dq_v = dU$

#  $q_v = \Delta U = n C_v \Delta T \Rightarrow \frac{f}{2} n R \Delta T = n C_v \Delta T$

$$C_v = \frac{f}{2} R$$



$$C_v = \left( \frac{du}{dT} \right)_v = \left( \frac{dq}{dT} \right)_v$$

⊕  $q_p = (\Delta H) \rightarrow$  Enthalpy change

$$dq_p = dH$$

$$\left( \frac{dH}{dT} \right)_p = C_p = \left( \frac{dq}{dT} \right)_p$$

⊕ Heat capacity (C)  $\rightarrow$  is process dependent

$\downarrow$   
J/°C  
or  
J/K

- $\rightarrow$  path function
- $\rightarrow$  Extensive property
- $\rightarrow$  Temp. dependent

If Temp. dependency is not given, take Heat capacity of substance as temp. independent.

## ⊕ First Law of Thermodynamics (FLOT)

"Energy is always conserved for universe."

or

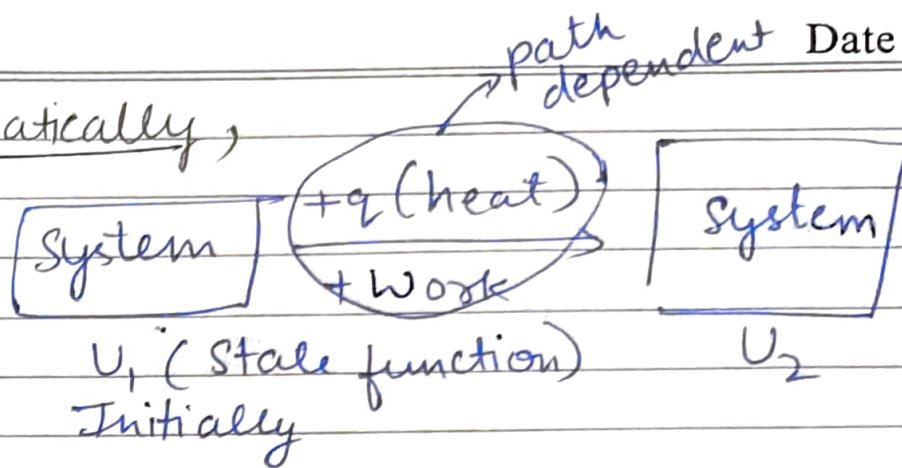
"Total energy for an isolated system remains constant."

or

"Energy can neither ~~not~~ be created nor be destroyed, it converts from one form to another form."

Spiral

Mathematically,



$$U_1 + q + W = U_2$$

$$U_2 - U_1 = q + W$$

$$\Delta U = q + W$$

$$\boxed{dU = \delta q + \delta W} \Rightarrow \text{Sum of two inexact differential can be exact differential}$$

or

$$\boxed{dU = dq + dW}$$

⊕ At const Volume Isochoric process

$$W=0 \quad \boxed{\Delta U = q_v}$$

Q → What is change in Internal energy ~~due~~ when 40 kJ work is done on system & 20 kJ heat is released by system?

Sol<sup>n</sup>

$$\Delta U = \boxed{q} + \boxed{W} \rightarrow +40 \quad \geq -20 + 40 = 20 \text{ kJ}$$

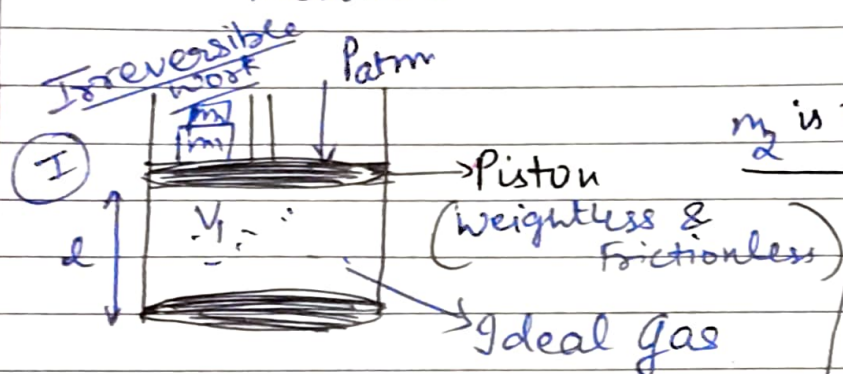
$\downarrow$   
-20



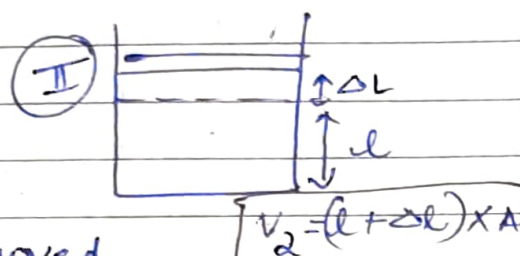
## # Work

$$W = \frac{F}{A} \times d \times A \quad \text{Volume displaced (for gases)}$$

Pressure



$$V_1 = l \times A$$

 $m_2$  is removed

$$P_g > (P_{ext})_1$$

gas expansion will occur till

$$2 \text{ Vol. of gas becomes } V_2. \quad P_g = (P_{ext})_2 = P_{atm} + \frac{m_1 g}{A}$$

Initially system is in Thermodynamic eq<sup>n</sup>.

$$P_g = (P_{ext})_1 = P_{atm} + \frac{(m_1 + m_2) g}{A}$$

$$W_{\text{single step}} = -P_{ext} \cdot \Delta V$$

Ext. Press. during that step

vol. change of Gas in single step.

$$W_{I \text{ to } II} = -(P_{ext})_2 \cdot \Delta V$$

$$= -(P_{ext})_2 \cdot (V_2 - V_1)$$

(#) Note - Irreversible single step work

$$= -P_{\text{ext}} \cdot \Delta V$$

$$= -P_{\text{ext}} (V_2 - V_1)$$

$$= -P_{\text{ext}} \left( \frac{nRT_2}{P_2} - \frac{nRT_1}{P_1} \right)$$

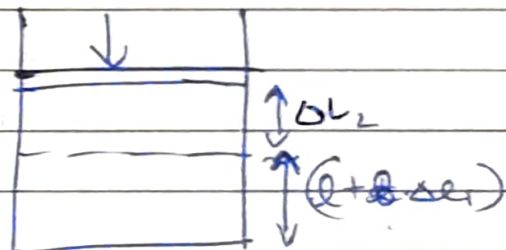
If process is complete,

$$P_{\text{ext}} = P_g$$

If  $m_1$  is removed  $\rightarrow$

gas expansion occurs (w. done by gas) to achieve  $(P_{\text{ext}})_3 = P_{\text{atm}}$

(III)



$$W_3 = (l + \Delta L_1 + \Delta L_2) \cdot A$$

$$W_{\text{II to III}} = (P_{\text{ext}})_3 (V_3 - V_2)$$

$$= -P_{\text{atm}} (V_3 - V_2)$$



# If Both  $m_1$  &  $m_2$  are simultaneously removed, then Vol. of gas changes from  $V_1 \rightarrow V_2$  under const. ext. Pressure of  $(P_{atm})$

$$W_{I to III} = -P_{atm}(V_2 - V_1)$$

~~$$W_{single\ step} = -P_{ext} \Delta V$$~~

# Note :-

Irreversible single step work

$$= -P_{ext} \cdot \Delta V$$

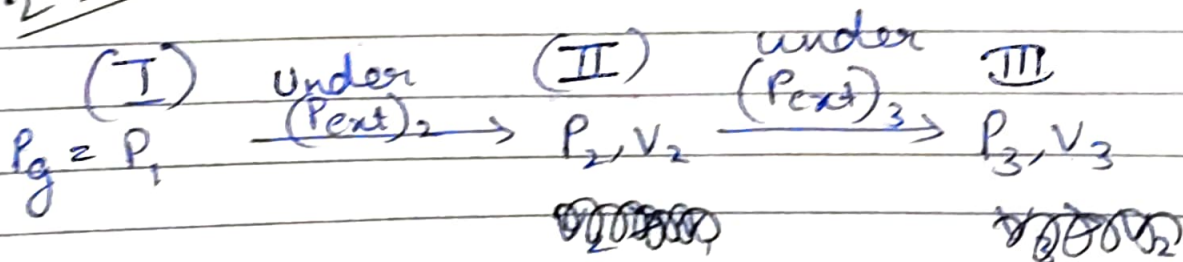
$$= -P_{ext} (V_2 - V_1)$$

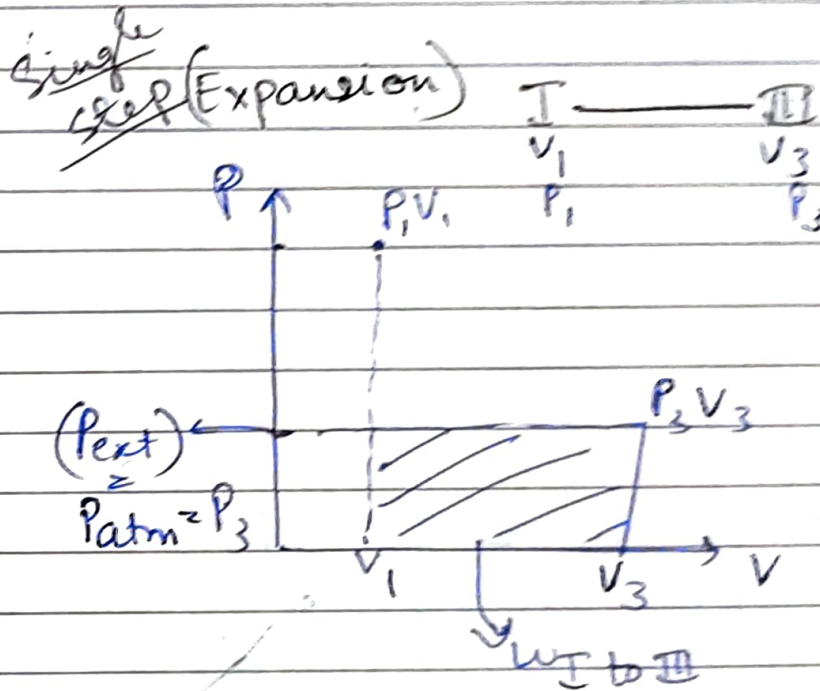
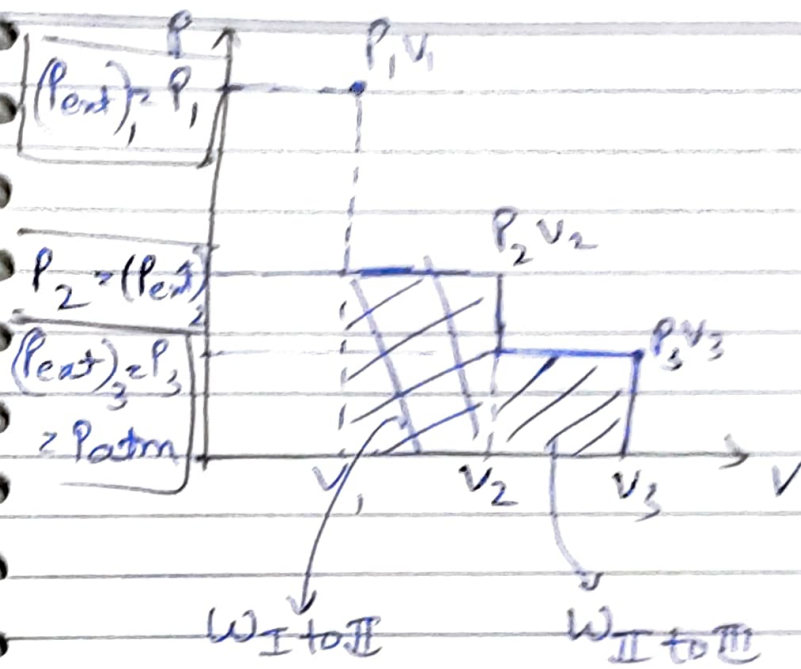
$$= -P_{ext} \left( \frac{nRT_2}{P_2} - \frac{nRT_1}{P_1} \right)$$

If Process is complete

$$P_{ext} = P_2$$

2 step work (Expansion)

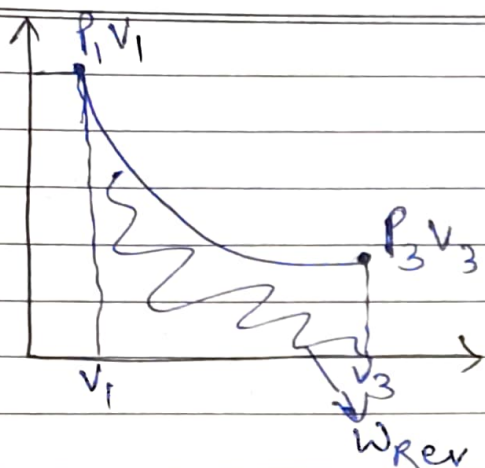




So, During Expansion (Irreversible)

$W_{\text{infinite steps}}$	$\dots$	$W_{3\text{-step}}$	$>$	$W_{2\text{-step}}$	$>$	$W_{\text{single step}}$
or						
$W_{\text{rev}}$	expansion		$W_{\text{irrev}}$ expansion			
Spiral						





$$\int dW_{rev} = - \int P_{ext} \cdot dV$$

$$P_{ext} = P_g \pm dp \quad \rightarrow \text{for single step}$$

$$dp \rightarrow 0$$

$$W_{rev} = - \int_{V_i}^{V_f} (P_g \pm dp) dV$$

$$W_{rev} = - \int_{V_i}^{V_f} P_g dV \quad \text{or} \quad \int dp dV \rightarrow 0$$

$$W_{rev} = - \int_{V_i}^{V_f} P_g dV = - \int_{V_i}^{V_f} \frac{nRT}{V} dV$$

works for  
both Exp or Compression

Note: Compression of Gas,  $V$  dec.  $\boxed{W = +ve}$

$$|W_{\text{single step}}| > |W_{\text{2-step}}| > \dots > |W_{\text{infinite step}}|$$

or  
 $|W_{rev}|$

# W-done in Various Process① Isothermal Process  $\Rightarrow T = \text{const.}$   $\Delta T = 0$ 

$$\Delta U = nC_v \Delta T = 0$$

$$\Delta U = 0$$

$$U = \text{const.}$$

$$q + w = 0$$

$$q_{\text{iso}} = -w_{\text{iso}}$$

$$\Delta H = nC_p \Delta T = 0$$

$$\Delta H = 0 \quad H = \text{const.}$$

H &amp; U

Both depends only on Temp. for Ideal Gas.

$$P_i V_i T$$

Initial state of ideal gas

$$P_f V_f T$$

final state of ideal gas

$$(a) (w_{\text{rev}})_{\text{iso}} = - \int_{V_i}^{V_f} \frac{nRT}{V} dV$$

$$= -nRT \int_{V_i}^{V_f} \frac{dV}{V} = -nRT \ln \left( \frac{V_f}{V_i} \right) = -nRT \ln \left( \frac{P_i}{P_f} \right)$$

or

$$= -2.303 nRT \log \left( \frac{V_f}{V_i} \right)$$

Boyle's law

$$P_i V_i = P_f V_f$$

$$\frac{V_f}{V_i} = \frac{P_i}{P_f}$$

Spiral

$$= -2.303 nRT \log \left( \frac{P_i}{P_f} \right)$$



$$\boxed{(q_{iso})_{rev} = (-W_{iso})_{rev}}$$

Q → find  $q$ ,  $\Delta U$ ,  $W$  when 2 mole of ideal undergoes Reversible isothermal process to change its state from (1 atm, 300K) to (3 atm, 300K)?

$$R = 0.0821 \text{ or } \frac{1}{12} \text{ L-atm mol}^{-1} \text{ K}^{-1}$$

Sol<sup>n</sup>

$$\Delta U = 0$$

$$q_{rev} = -W_{rev}$$

$$W_{rev} = -2.303 n RT \log \left( \frac{P_i}{P_f} \right)$$

$$= -2.303 \times 2 \times 0.0821 \times 300 \times \log \left( \frac{1}{3} \right)$$

$$= + 2.303 \times 2 \times 0.0821 \times 300 \times 0.47 \text{ L-atm}$$

$$1 \text{ L-atm} = 101.325 \text{ Joule}$$

$$\log 2 = 0.3$$

$$\log 3 = 0.47$$

$$\log 5 = 0.7$$

$$\log 7 = 0.84$$

$$\log 11 = 1.043$$

$(W_{rev})_{\text{compression}}$

$$= 2.303 \times 2 \times 0.0821 \times 300 \times 0.47$$

$$\times 101.325 \text{ Joules}$$

(b) single step

$$W_{irr} = -P_{ext} (V_f - V_i)$$

$$= -P_{ext} \left( \frac{nRT_f}{P_f} - \frac{nRT_i}{P_i} \right)$$

$$(W_{irr})_{iso} = -P_{ext} nRT \left[ \frac{1}{P_f} - \frac{1}{P_i} \right]$$

\*\* When Exp or compression completes

$$P_{ext} = P_f$$

$$(W_{irr})_{iso} = -nRT \left[ 1 - \frac{P_f}{P_i} \right]$$

Q → find  $\Delta U$  when 20 kJ heat is given to ideal Gas & gas expands under Ext Press. of 2 atm from 3 dm<sup>3</sup> to 5 dm<sup>3</sup>?

Sol<sup>n</sup>

$$\Delta U = q + w$$

$$\Delta U = 20 - P_{ext} \Delta V$$

$$= 20 \text{ (kJ)} - \underbrace{2}_{2\text{-atm}} (5-3)$$

$$\Delta U = 20 \times 10^3 \text{ J} - (2 \times 2 \times 101.325) \text{ J}$$



## ② Adiabatic Process

$$P_1 V_1 T_1 \rightarrow P_2 V_2 T_2$$

$\Rightarrow$  System having ideal Gas is isolated

$\Rightarrow q = 0 \rightarrow$  Heat exchange = 0

$$\Rightarrow \Delta U = q + w$$

$$\Delta U = w_{ad} = n C_v (T_2 - T_1) \rightarrow \text{Rev or Irr.}$$

~~Adiabatic process~~

$$C_p - C_v = R$$

$$\frac{C_p}{C_v} - \frac{C_v}{C_v} = \frac{R}{C_v}$$

$$\gamma - 1 = \frac{R}{C_v}$$

$$C_v = \frac{R}{(\gamma - 1)}$$

$$w_{ad} = \frac{nR}{(\gamma - 1)} \left[ \frac{P_2 V_2}{nR} - \frac{P_1 V_1}{nR} \right]$$

$$w_{ad} = \frac{P_2 V_2 - P_1 V_1}{(\gamma - 1)} = \frac{\Delta(PV)}{(\gamma - 1)}$$

# Adiabatic Exp. of Gas

$$\rightarrow W_{ad} = -ve$$

$$nC_v(T_2 - T_1) = -ve$$

$$(T_2 < T_1) \quad T \downarrow \text{es, Cooling}$$

# Adiabatic Compression of Gas

$$W_{ad} = +ve$$

$$\Delta T = +ve$$

$$(T_2 > T_1) \quad T \uparrow \text{es, Heating}$$

# If During Calculation of Work, any parameter is not given then, we must know whether Process is Rev. or Irr. .

(a) Process is Rev. Ad.

$$dU = (dW_{ad})_{rev}$$

$$nC_v dT = - \int nRT \frac{dV}{V}$$

$$nC_v \int \frac{dT}{T} = - nR \int \frac{dV}{V}$$



$$nC_V \ln\left(\frac{T_2}{T_1}\right) = -nR \ln\left(\frac{V_2}{V_1}\right)$$

$$\ln\left(\frac{T_2}{T_1}\right) = -\frac{R}{C_V} \ln\left(\frac{V_2}{V_1}\right)$$

$$\ln\left(\frac{T_2}{T_1}\right) = (\gamma - 1) \ln\left(\frac{V_2}{V_1}\right)$$

$$\left(\frac{T_2}{T_1}\right) = \left(\frac{V_1}{V_2}\right)^{(\gamma - 1)}$$

$$TV^{\gamma-1} = \text{const.}$$

Similarly,

$$PV^{\gamma} = \text{const.}$$

$$T^{\gamma} P^{1-\gamma} = \text{const.}$$

(b) Irr. Ad

$$\Delta U = W_{ad}$$

$$nC_V(T_2 - T_1) = -P_{ext}(V_2 - V_1)$$

$$nC_V(T_2 - T_1) = -P_{ext} \left( \frac{nRT_2}{P_2} - \frac{nRT_1}{P_1} \right)$$

Q → 3 mole of non-linear triatomic Gas undergoes adiabatic process such that state of Gas changes from

$$\boxed{16 \text{ atm}, 300 \text{ K}} \longrightarrow \boxed{1 \text{ atm}, T \text{ (K)}}$$

2 work

find  $T$  if (i) Process is Reversible

(ii) Process is Irreversible

Sol<sup>n</sup> (i) Reversible

$$W_{\text{ad}} = nC_V(T_2 - T_1) = 3 \times 3R [T - 300]$$

T value for Reversible Process

$$T^\gamma P^{1-\gamma} = \text{const.}$$

$$T_1^\gamma P_1^{1-\gamma} = T_2^\gamma P_2^{1-\gamma}$$

$$\left(\frac{T_2}{T_1}\right)^\gamma = \left(\frac{P_1}{P_2}\right)^{\frac{1-\gamma}{\gamma}} \Rightarrow T_2 = T_1 \left[\frac{P_1}{P_2}\right]^{\frac{1-\gamma}{\gamma}}$$

$$T = T_2 = 300 \left[\frac{16}{1}\right]^{\frac{1-\frac{4}{3}}{\frac{4}{3}}} = 300 \left(2^4\right)^{\frac{1}{4}}$$

$$= 300 (2^4)^{\frac{1}{4}}$$

$$= \frac{300 \times 2}{2} = \boxed{150 \text{ K}}$$



$$(W_{ad})_{Rev} = 3 \times 3R [150 - 300] = 9R \times (-150) \text{ Joules}$$

(ii) Process is Irr

$$(W_{ad})_{irr} = 3 \times 3R (T - 300)$$

T is calculated from irreversible path using eq<sup>n</sup> (1) or (2)

$$-1 \times R \left[ \frac{T}{1} - \frac{300}{16} \right] = 3R [T - 300]$$

$$T \approx 236 \text{ K}$$

$$(W_{ad})_{irr} = 3 \times 3R (T - 300)$$

$$= 3 \times 3R (230 - 300) \\ = 9R (-70)$$

(cooling)

Conclusion

Initial state

$P_1, V_1, T_1$

Adiabatic

Rev. Exp.

$P_2, V_2, (T_{rev})_{final}$

(cooling)

Ad

Irr Exp

$$|(\Delta T)_{rev}| > |(\Delta T)_{irr}|$$

$P_2, V_2, (T_{irr})_{final}$   
( $\Delta T_{rev}$ )

$$T_1 > (T_{irr})_{final} > (T_{rev})_{final}$$

( $\Delta T$ )<sub>irr</sub>

# ① Comparison b/w Iso & Adiabatic

$$\text{Expansion } |W_{\text{iso}}| > |W_{\text{ad}}| \quad (\text{Rev. or Irr.})$$

## ② Isochoric Process

$$V = \text{const.}$$

$$\Delta V = 0$$

$$W = 0$$

from FLOT

$$q + w = \Delta U$$

$$q_v = \Delta U = nC_v \Delta T$$

## ④ Isobaric Process

$$P = \text{const.}$$

$$dw = -P_{\text{ext}} dv$$

$$W = -P \int dv$$

$$W = -P \Delta V$$

$$\boxed{W = -P \Delta V}$$

$$W = -nR \Delta T$$

→ gas undergoes expansion or compression

① for  $Rx^n$   
 $T, P, V \rightarrow$  kept const. when  
 we set any  $Rx^n$ .

Work done in case of  $Rx^n$  is due to change in





## # H (Enthalpy)

↳ State function

↳ Extensive property

↳ Defined as  $H = U + PV$

$$dH = dU + d(PV)$$

$$dH = dU + PdV + VdP \quad \text{at const. } P$$

from FLOT

$$dq + dw = dU$$

$$dq_p - PdV = dU$$

$$dq_p = dU + PdV$$

at const.  $P$

$$dH = dq_p \Rightarrow q_p = \Delta H$$

heat exchange b/w system & surrounding at const  $P$  is enthalpy change

a) Nothing is const.

$$dH = dU + d(PV)$$

$$\Delta H = \Delta U + \Delta(PV)$$

$$\Delta H = \Delta U + (P_2V_2 - P_1V_1)$$

for ideal gas

$$\Delta H = \Delta U + (nRT_2 - nRT_1)$$

$$\Delta H = \Delta U + nR(T_2 - T_1)$$



b) at const P,  $\Delta H = \Delta U + P\Delta V$

Ideal Gas  
undergoing any  
Process

$$\Delta H = \Delta U + nR\Delta T$$

(Exp or Comp.)

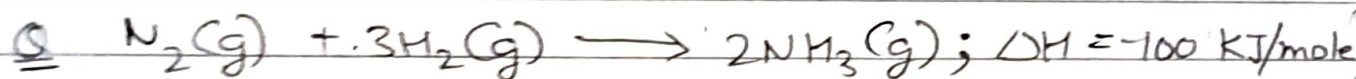
c) for Rxn involving Ideal Gases

$$P\Delta V = \Delta n_g RT$$

$$\Delta H = \Delta U + \Delta n_g RT$$

$$\Delta H - \Delta U = \Delta n_g RT$$

$$q_p - q_v = \Delta n_g RT$$



a) find heat evolved at const. Volume at 300K?

$$q_v = \Delta U$$

$$\Delta H = \Delta U + \Delta n_g RT$$

$$\Delta U = \Delta H - \Delta n_g RT$$

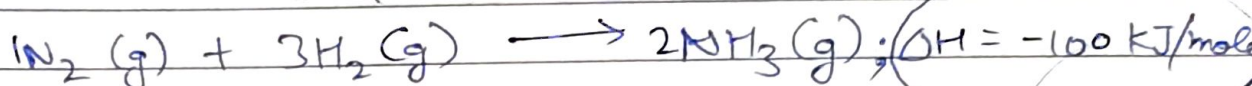
$$\Delta n_g = 2 - (3+1) = -2$$

Difference of stoichiometric  
coeff. of product & reactant

$$\Delta U = \Delta H + 2RT$$

$$= [-100000 + 2 \times 8.314 \times 300] \text{ Joule}$$

b) find heat evolved at const. Volume when 4 moles of  $N_2$  and 12g of  $H_2$  reacts at 300K?



$$\begin{array}{r} 4 \text{ mole} \\ = 2 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 12 = 6 \text{ mole} \\ 2 \\ \hline -6 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 0 \\ + 4 \\ \hline 4 \end{array}$$

Acc. to  
Stoich. coeffs.  
of (L.R)

$$\Delta U = \Delta H - \Delta n_g RT$$

$$\Delta U = [-100 \times 10^3 - (-2)RT]$$

w.r.t 3 moles of L.R

$$\text{w.r.t 3 mole of L.R} \rightarrow \Delta U = [-100 \times 10^3 + 2RT]$$

$$\text{" 1 mole " " } \rightarrow \Delta U = \frac{[-100 \times 10^3 + 2RT]}{3}$$

$$\text{" 6 mole " " } \rightarrow \Delta U = \frac{(-100 \times 10^3 + 2RT) \times 6}{3}$$

## # Thermochemistry

→ We will deal with  $\Delta H$  of various Rxns/  
phase change

$$\Delta H_{Rx} = -ve \text{ (Exo)}$$

$$\Delta H_{Rx} = +ve \text{ (Endo)}$$

## (I) Std. Enthalpy of formation ( $\Delta H_f^\circ$ )

Spiral

Temp. usually  
taken 25°C

P = 1 bar  
Conc = 1 mole/l

Standard state



Enthalpy change (usually -ve) when 1 mole substance (s, l, g) is formed from its constituent elements present in their most stable form at std. state.

$$\Delta H_f^\circ (\text{Elemental form}) = 0$$

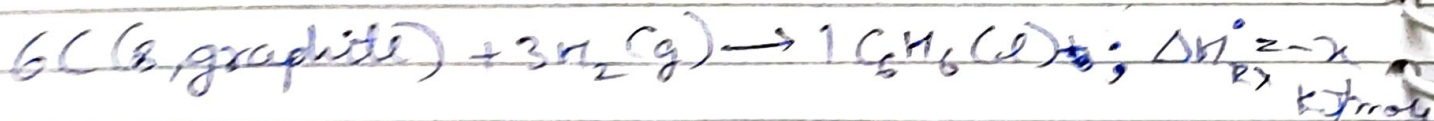
- $\Delta H_f^\circ (\text{C, s, graph.}) = 0$
  - $\Delta H_f^\circ (\text{C, s, diamond}) \neq 0$
  - $\Delta H_f^\circ (\text{H}_2, \text{g}) = 0$
  - $\Delta H_f^\circ (\text{H, g}) \neq 0$
  - $\Delta H_f^\circ (\text{S}_8, \text{rhombic}) = 0$
  - $\Delta H_f^\circ (\text{S}_8, \text{Monoclinic}) \neq 0$
  - $\Delta H_f^\circ (\text{H}^+, \text{aq.}) = 0$  (Assume)
  - $\Delta H_f^\circ (\text{OH}^-, \text{aq.}) \neq 0$
- rhombic is more stable than Monoclinic form at RT (25°C)

- $\Delta H_f^\circ (\text{Br}_2, \text{l}) = 0$
- $\Delta H_f^\circ (\text{Br}_2, \text{g}) \neq 0$
- $\Delta H_f^\circ (\text{O}_2, \text{g}) = 0$
- $\Delta H_f^\circ (\text{Cl}_2, \text{g}) \neq 0$
- $\Delta H_f^\circ (\text{O}_2, \text{g}) = 0$

Exception

$$\begin{aligned} \Delta H_f^\circ (\text{White P.}) &= 0 \\ \Delta H_f^\circ (\text{Red P.}) &\neq 0 \\ \Delta H_f^\circ (\text{Black P.}) &\neq 0 \end{aligned}$$

stability order = white P < Red P < Black P



$$\Delta H_f^\circ (\text{C}_6\text{H}_6, \text{l})$$

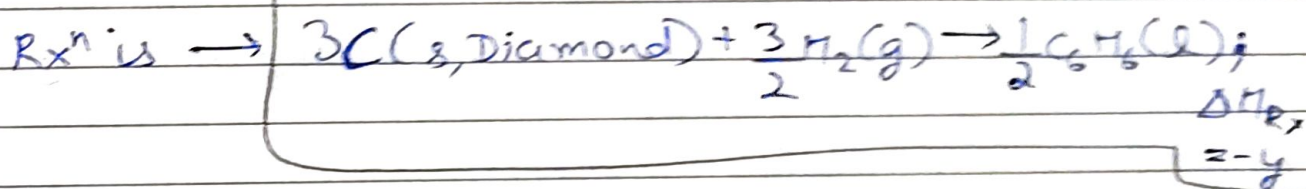
$$-x = \Delta H_{R, \text{KJ/mole}}^\circ = 1 \Delta H_f^\circ (\text{C}_6\text{H}_6) - [6 \cancel{\Delta H_f^\circ (\text{C, s, graph.})} + 3 \cancel{\Delta H_f^\circ (\text{H}_2)}]$$

Note - for any Rxn

$$\Delta H_{Rxn} = \sum \Delta H_f(\text{Products}) - \sum \Delta H_f(\text{Reactants})$$

Q find  $\Delta H_f$  (~~of~~) ( $C_6H_6$ )?

$$\Delta H_f(C, s, \text{Diamond}) = -x \text{ kJ/mole}$$



Sol<sup>n</sup>  $\Delta H_{Rxn} = -y = \frac{1}{2} \Delta H_f(C_6H_6) - 3 \Delta H_f(C, s, \text{diamond}) - \frac{3}{2} \Delta H_f(H_2, g)$

$$-y = \frac{1}{2} \Delta H_f(C_6H_6) - 3(-x)$$

$$2(-3x - y) = \Delta H_f(C_6H_6)$$

②  $\Delta H_c^\circ$  (Std. Enthalpy of Combustion)

↳ Enthalpy change (usually -ve) when 1 mole substance (s, l, g) is completely burnt in oxygen at Std. State.



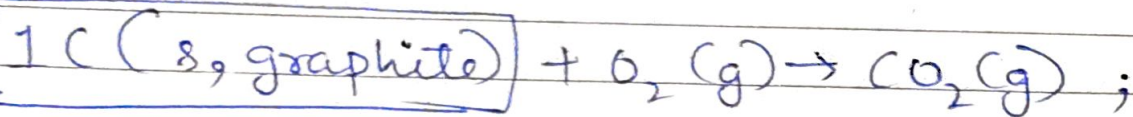
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$\Delta H_c = +ve$  only  
for  $F_2, N_2, N_2O$

$$\Delta H_c(O_2) = 0$$

$$\Delta H_c(CO_2) = 0$$

$$\Delta H_c(H_2O) = 0$$



$$\Delta H_R^\circ = -x = \Delta H_c^\circ(C, s, \text{graphite})$$

$$= \Delta H_f^\circ(CO_2, g)$$

Note:- for any  $R_x^n$

$$\Delta H_R = \sum \Delta H_c(\text{Reactants}) - \sum \Delta H_c(\text{Products})$$

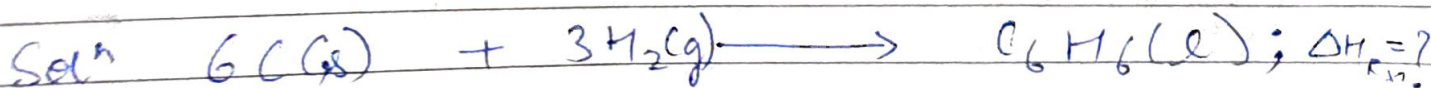
$$\Delta H_R = \Delta H_c(C, s, \text{grap}) + \cancel{\Delta H_c(CO_2)} - \cancel{\Delta H_c(CO_2)}$$

$$\Rightarrow \Delta H_f(C_6H_6, l) = ?$$

$$\Delta H_c(C_6H_6, l) = -x$$

$$\Delta H_c(H_2, g) = -y$$

$$\Delta H_c(C, s, \text{graphite}) = -z$$



$$6\Delta H_c(C, s) + 3\Delta H_f(H_2O) - \Delta H_f(C_6H_6) = 1 \times \Delta H_f(C_6H_6) - [6\Delta H_f(C, s) + 3\Delta H_f(H_2O)]$$

$$6(-z) + 3(-y) - (-x) = \Delta H_f(C_6H_6)$$

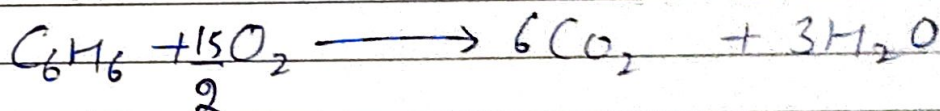
$$\boxed{-6z - 3y + x = \Delta H_f(C_6H_6)}$$

Q  $\rightarrow \Delta H_c(C_6H_6, l) = ?$

$$\Delta H_f(CO_2) = -x$$

$$\Delta H_f(H_2O) = -y$$

$$\Delta H_f(C_6H_6) = -z$$



$$\Delta H_c(C_6H_6, l) = 6\Delta H_f(CO_2) + 3\Delta H_f(H_2O) - \Delta H_f(C_6H_6) - \cancel{\Delta H_f(O_2)}$$

$$= 6(-x) + 3(-y) - (-z)$$

$$= -6x - 3y + z$$

Q If  $x$  gm Benzene on combustion releases  $y$  kJ of heat. find enthalpy of combustion of Benzene?

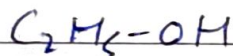


Sol<sup>n</sup>  $\left( \frac{x}{\text{molar mass of Benzene}} \right) \text{ moles} \longrightarrow -y \text{ KJ}$

1 mole  $\longrightarrow \frac{-y}{x/M} \Rightarrow \frac{-yM}{x} \text{ KJ/mole}$   $\xrightarrow{\Delta H_c(\text{Benzene})}$

(#) Calorific value (cv) of substance  $\xrightarrow{\text{Unit J/g or KJ/g or Cal/g}}$   
 $\hookrightarrow$  Heat evolved by combustion of 1gm substance.

(\*\*) C.V of substance =  $\frac{\Delta H_c(\text{Substance})}{\text{Molar mass of substance}}$



Q  $\rightarrow \Delta H_c(\text{Ethanol}) = -x \text{ KJ/mole}$   
 find C.V of ethanol?

Sol<sup>n</sup> 1 mole  $\longrightarrow \Delta H_c = -x$   
 $\hookrightarrow 46 \text{ g}$

1g  $\longrightarrow \left( \frac{-x}{46} \right) = \text{C.V}$

(3)  $\Delta H_{\text{neutralization}}$   $\xrightarrow{-ve}$

Std. enthalpy change

when 1 equivalent or 1gm-eq. Acid is neutralised

by 1 gm-eq of Base

$$\text{gm-eq} = \text{mole} \times n.f$$

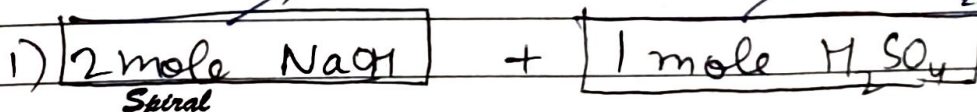
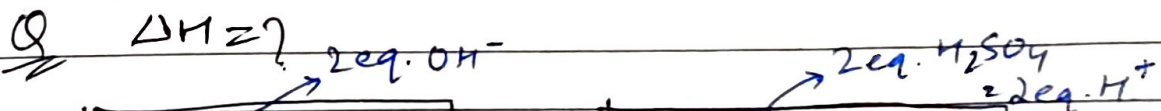
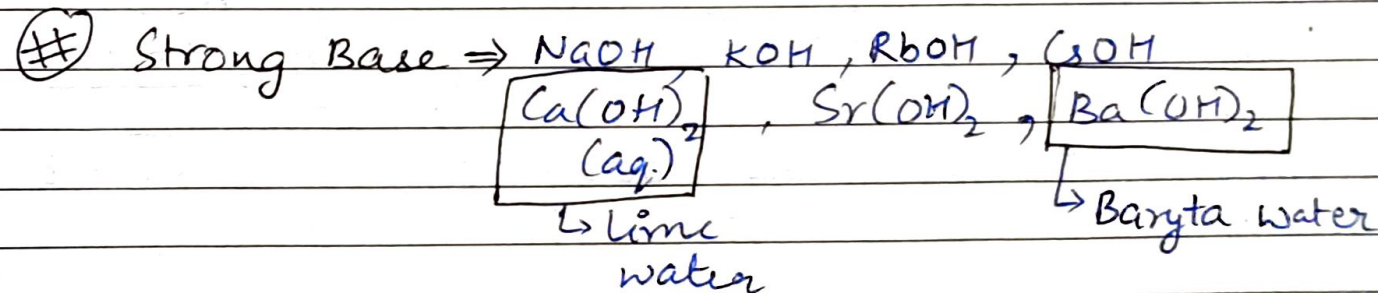
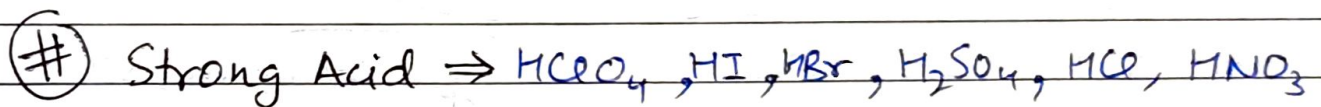
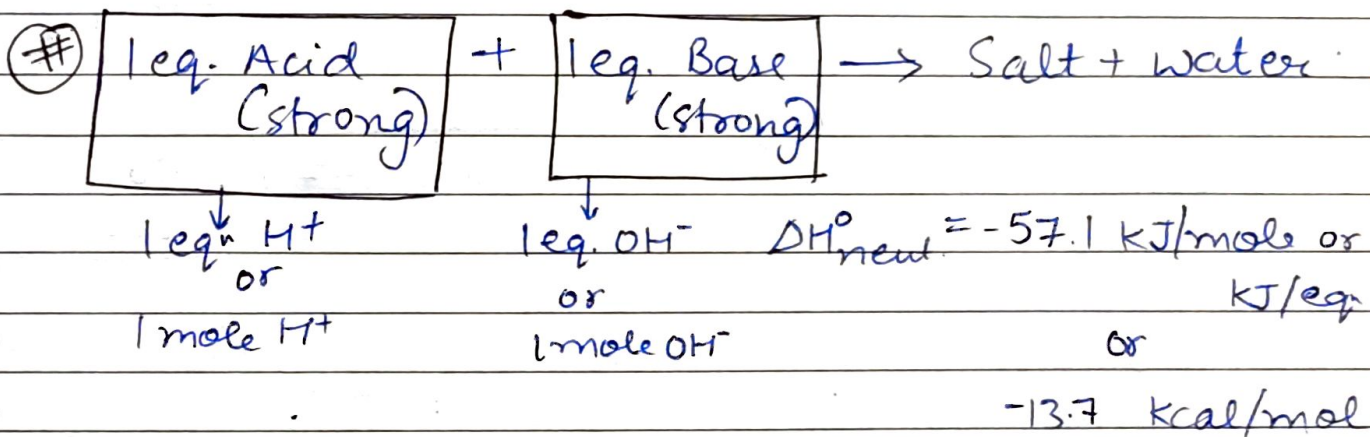
or  
eq

$$\text{equivalent of Strong Acid} = \text{eq of } H^+ = \text{mole of } H^+$$

$$\text{equivalent of Strong Base} = \text{eq of } OH^- = \text{mole of } OH^-$$

$$\text{eq.} = N \times V_{\text{soln}} (L) \quad \boxed{N = M \times n.f}$$

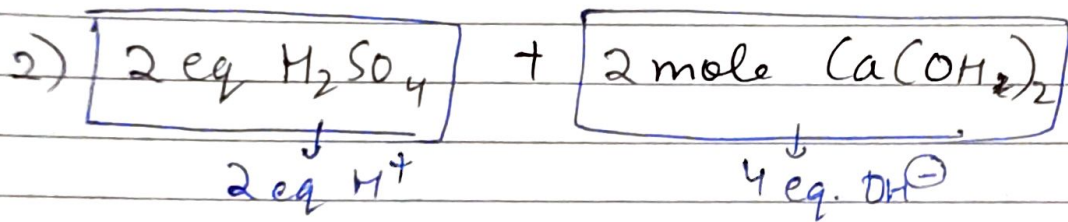
$$\text{meq.} = N \times V_{\text{soln}} (ml)$$



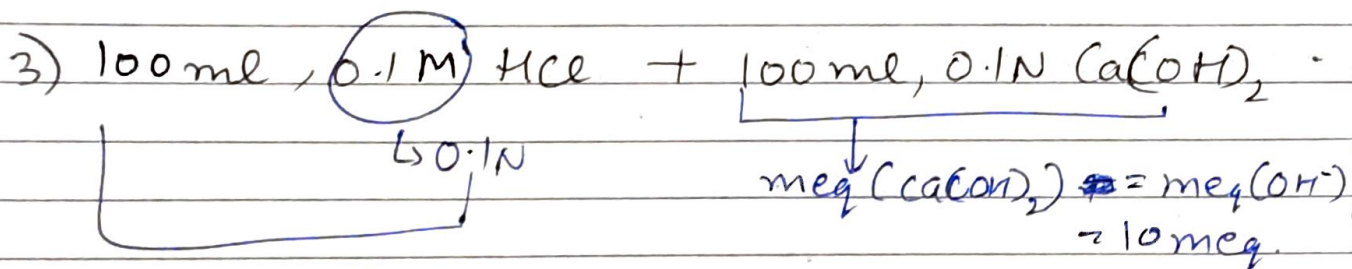


Soln

$$\Delta H = (-57.1 \times 2) \text{ kJ}$$



$$\Delta H^\circ (-571 \times 2) \text{ kJ}$$



$$\text{meq} = \text{meq}(\text{H}^+) = 100 \times 0.1$$
$$(\text{HCl}) = 10 \text{ meq}$$

$$\Delta H = -57.1 \times \frac{10}{1000} \text{ kJ}$$

$\rightarrow 10 \text{ meq.}$

Q → find rise in temp. when 100 ml, 0.1 M NaOH reacts with 100 ml, 0.1 M H<sub>2</sub>SO<sub>4</sub>?  
↳ 0.2 N → 20 meq.

$$\begin{aligned} s(\text{water}) &= 4.2 \text{ J K}^{-1} \text{ gm}^{-1} \\ \rho_{\text{H}_2\text{O}} &= 1 \text{ g/ml} \end{aligned}$$

$$q_p = \Delta H = m_s \Delta T = n C \Delta T$$

$$V_{H_2O} = 200 \text{ ml}$$

$$\rho_{H_2O} = \frac{m}{V_{H_2O}} \quad [m = 200 \text{ g}]$$

$$\Delta H = \left| -57.1 \times \frac{10}{1000} \times 1000 \text{ J} \right| = \text{heat absorbed by water}$$

$$-57.1 \times 10 = m \alpha g \times \Delta T$$

$$\frac{571 \times 10}{200 \times 42} = \Delta T$$

#### (4) Enthalpy of ionization ( $\Delta H_i$ )

heat or enthalpy (+ve) change to convert or dissociate 1 mole weak electrolyte (Weak Acid or Weak Base) completely into ions

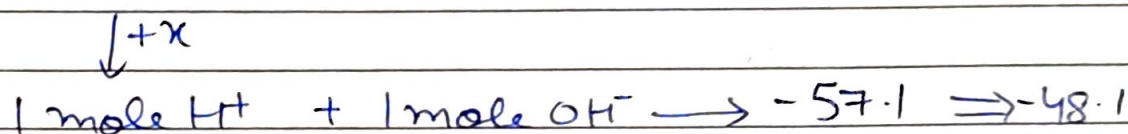
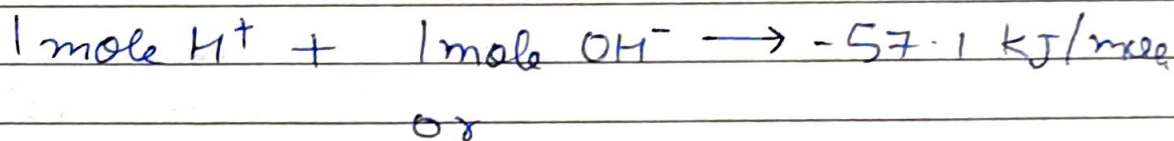
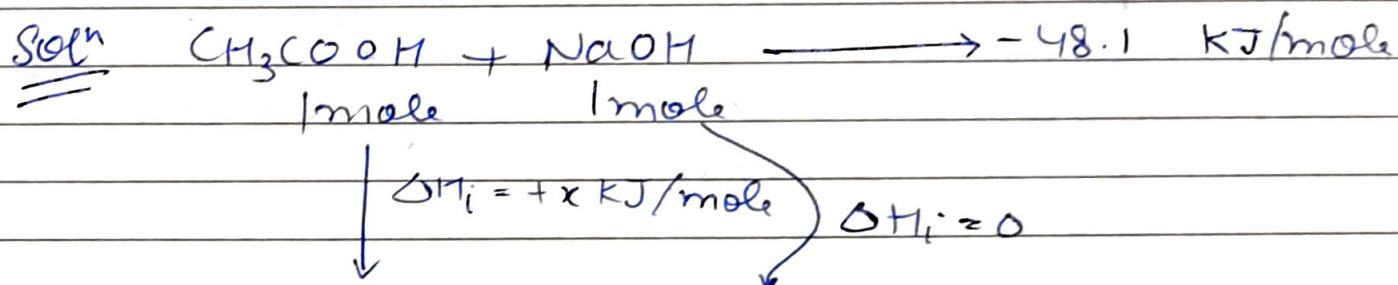
$$\Delta H_i \text{ (strong, electrolyte)} = 0$$

S.A, S.B, all salt

$$\Delta H_i \text{ (Weak Electrolyte)} \neq 0$$

Q  $\Rightarrow \Delta H_i \text{ (CH}_3\text{COOH)} = ?$

if 1 mole of  $\text{CH}_3\text{COOH}$  is mixed with 1 mole  $\text{NaOH}$  & heat of neutralization is  $-48.1 \text{ kJ}$ .

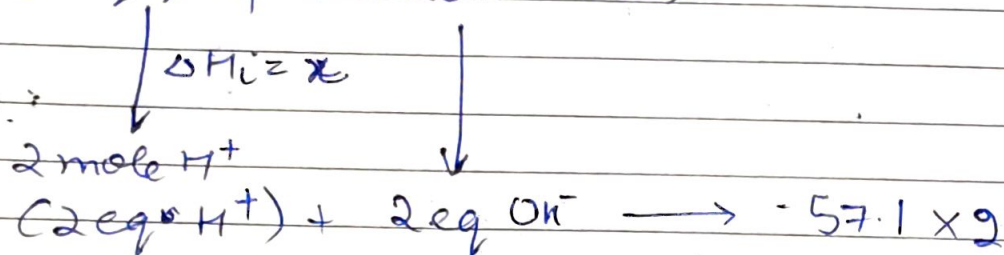
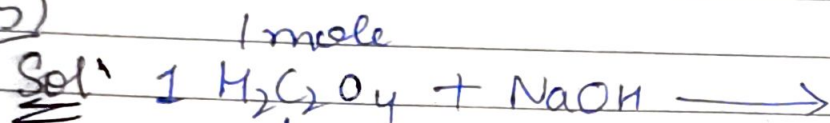


$$x + (-57.1) = -48.1$$

$$\boxed{x = 9 \text{ kJ/mole}}$$



Q-5)



$$x - (-57.1 \times 2) = (-53.35 \times 2)$$

$$x = 8$$

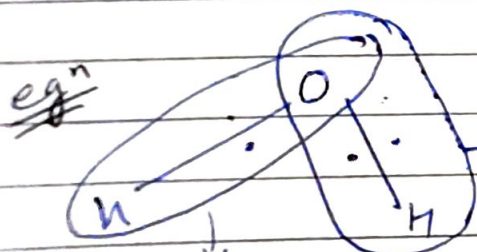
# Concept of Bond dissociation enthalpy and Bond energy

B.E  $\Rightarrow$  Average  
 Energy required  
 to Break 1 mole  
 Bond.

B.D.E

Energy required to  
 Break 1 mole of  
 any covalent Bond.

B.E (Bond Enthalpy) is used when any Bond is repeated more than once in any compound.



$$\text{B.d.e. (OH-Bond)} = x_1$$

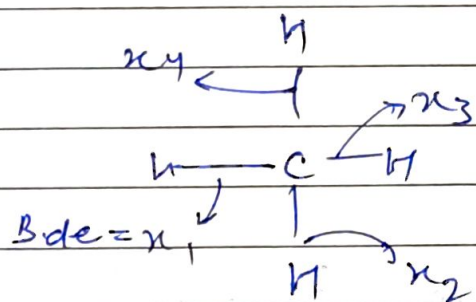
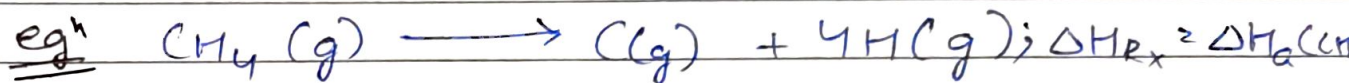
$$\text{B.d.e.}_2 (\text{O-H}) = x_2$$

$$\text{B.E (O-H)} = \frac{\text{B.d.e.}_1 + \text{B.d.e.}_2}{2} = \frac{x_1 + x_2}{2}$$

Note:-  $\Delta H_a$  (Enthalpy of atomization)

enthalpy change when 1 mole of any substance  
(+) -nce  
(s, l, g)

is completely converted gaseous atoms.



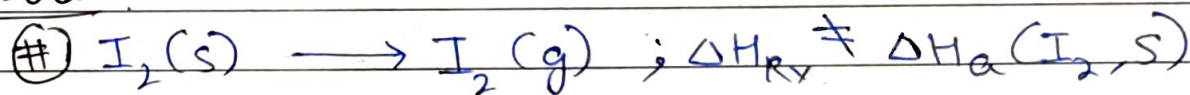
$$= x \text{ kJ/mole}$$

$$= x_1 + x_2 + x_3 + x_4$$

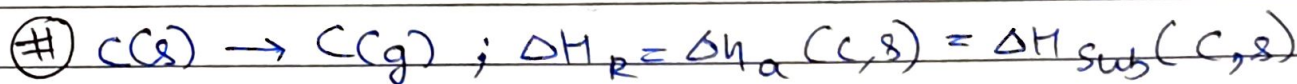
$$\text{B.E (C-H)} = \frac{x_1 + x_2 + x_3 + x_4}{4}$$

$$= \frac{x}{4} = \frac{\Delta H_a(\text{CH}_4)}{4}$$

Note +



$$\Delta H_{\text{Rx}} = \Delta H_{\text{sublimation}}(\text{I}_2, \text{s})$$



Note :-  $\Delta H$  of any  $\text{Rx}^n$  can be represented in terms of B.E data of Reactants and Products (Provided Reactants & Products are present in Gaseous state)



$$\Delta H_{rx} = \sum \text{B.E data of Reactants} - \sum \text{B.E data of Products}$$

## Q Combustion of $\text{CH}_4$

$$\Delta H_c(\text{CH}_4) = ?$$

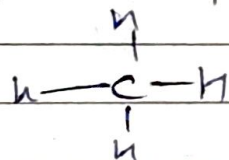
Given :- B.E (C-H) =  $x_1$  kJ/mole

B.E (O=O) =  $x_2$  "

B.E (C=O) =  $x_3$  "

B.E (O-H) =  $x_4$  "

$\Delta H_{\text{vap}}$  ~~for~~ ( $\text{H}_2\text{O}, \ell$ ) =  $x_5$  "



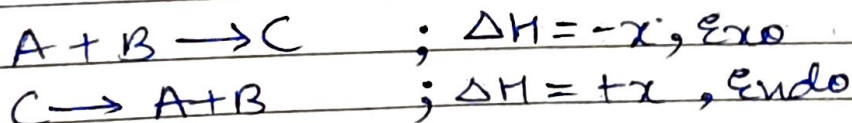
$$\Delta H_{rx} = \Delta H_c(\text{CH}_4) = ?$$

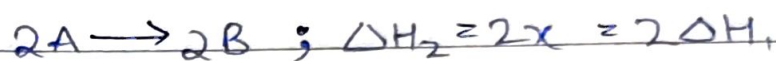
$$\Delta H_c(\text{CH}_4) = \Delta H_{rx} = 4\text{B.E}(\text{C-H}) + 2\text{B.E}(\text{O=O})$$

$$\left[ 2\text{B.E}(\text{C=O}) + 2\Delta H_{\text{vap}}(\text{H}_2\text{O}) + 4\text{B.E}(\text{O-H}) \right]$$

## # Laws of Thermochemistry :-

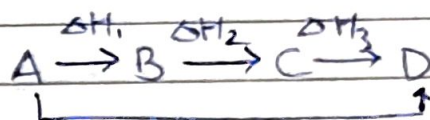
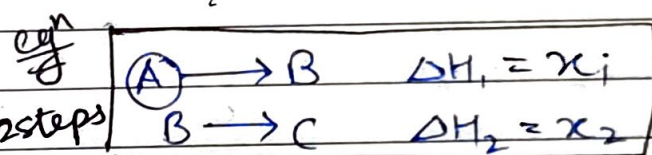
① Lavoisier law  $\rightarrow$  Reversing the rxn Enthalpy change sign reverses



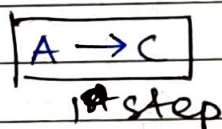


Imp.

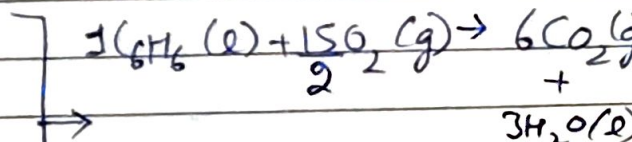
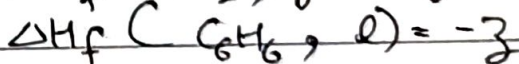
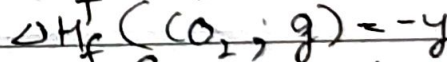
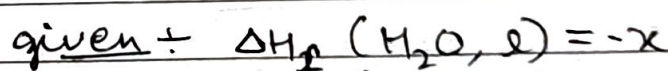
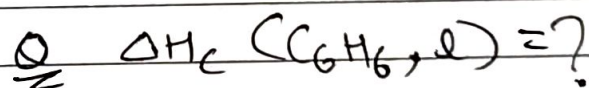
③ Hess's law  $\rightarrow$  The enthalpy change in a chemical or physical process is same whether the process is carried out in one step or in several steps.



$$x = \Delta H_{\text{net}} = \Delta H_1 + \Delta H_2 + \Delta H_3$$



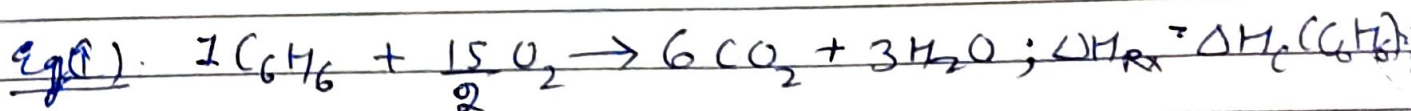
$$\Delta H = \Delta H_1 + \Delta H_2 = x_1 + x_2$$



$$\Delta H_{rx} = \Delta H(C_6H_6)$$

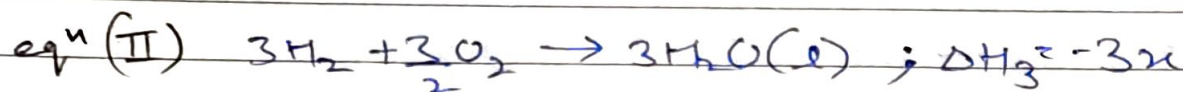
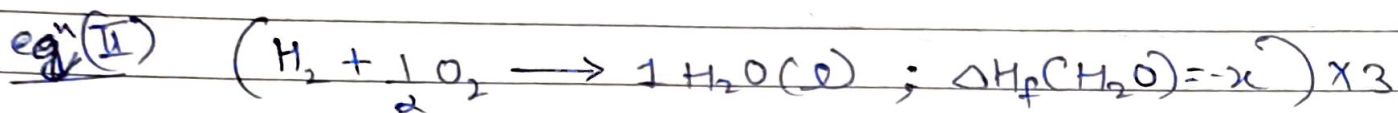
$$\Delta H_c(C_6H_6) = -3x - 6y + 3z$$

Sol<sup>n</sup> Combustion of Rx<sup>n</sup> for  $C_6H_6$

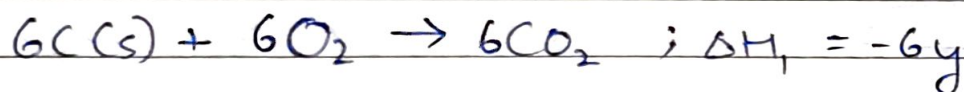
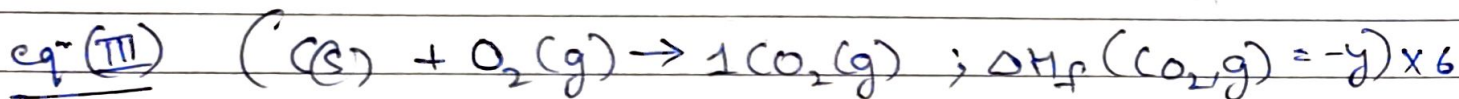




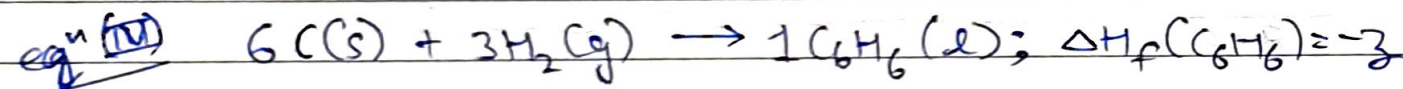
Given  $\div$   $H_2O$  formation  $\div$



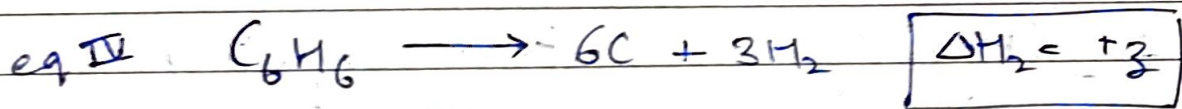
$CO_2$  formation



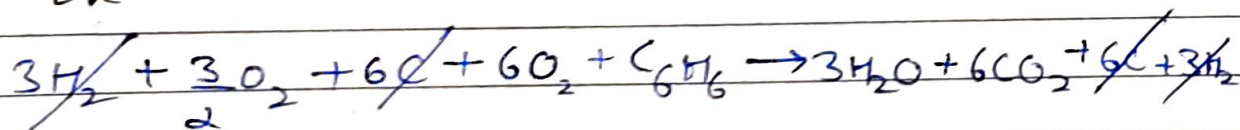
$C_6H_6$  formation  $\div$



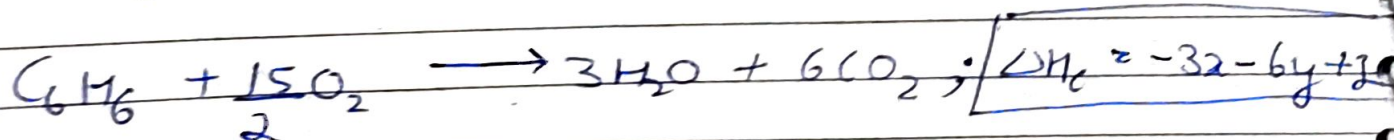
Reverse Eq IV



Add eq<sup>n</sup> III + eq<sup>n</sup> IV + eq<sup>n</sup> II



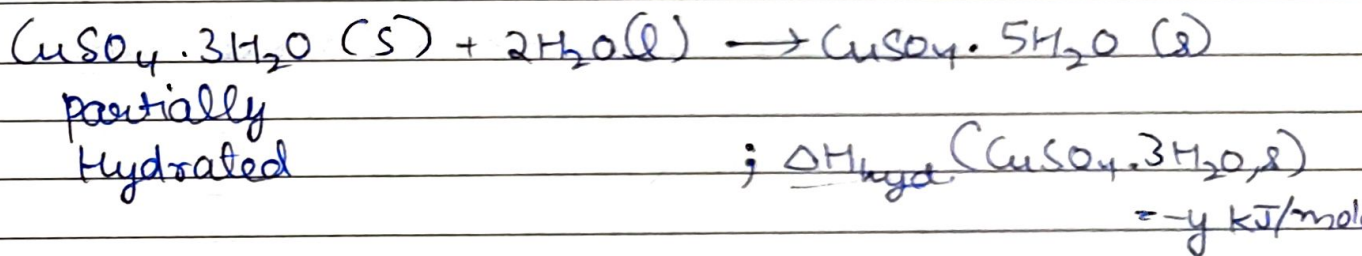
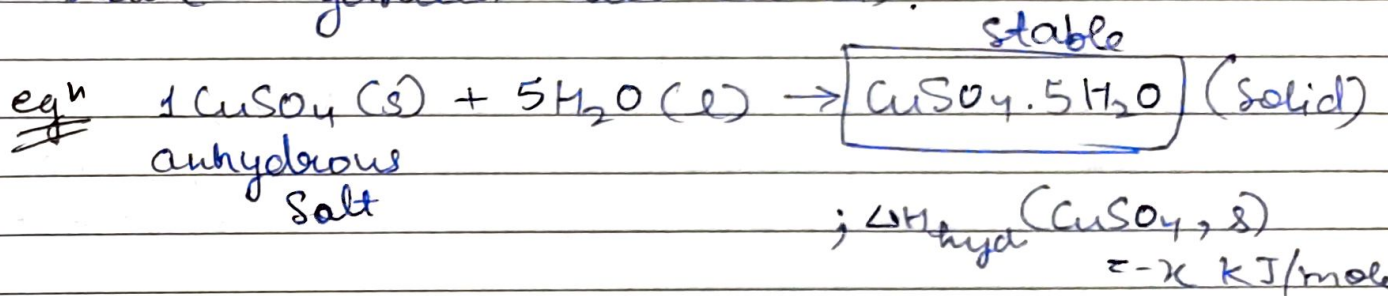
$\Delta H_c(C_6H_6) \Rightarrow \Delta H_{net} = -3x - 6y + z$



### (3) Enthalpy of Hydration of Compound ( $\Delta H_{\text{hyd}}$ )

no water

Enthalpy change when 1 mole of a given anhydrous or partially Hydrated Salt is allowed to combine with required no. of moles of water molecules to form a specific stable Hydrated Salt (solid).

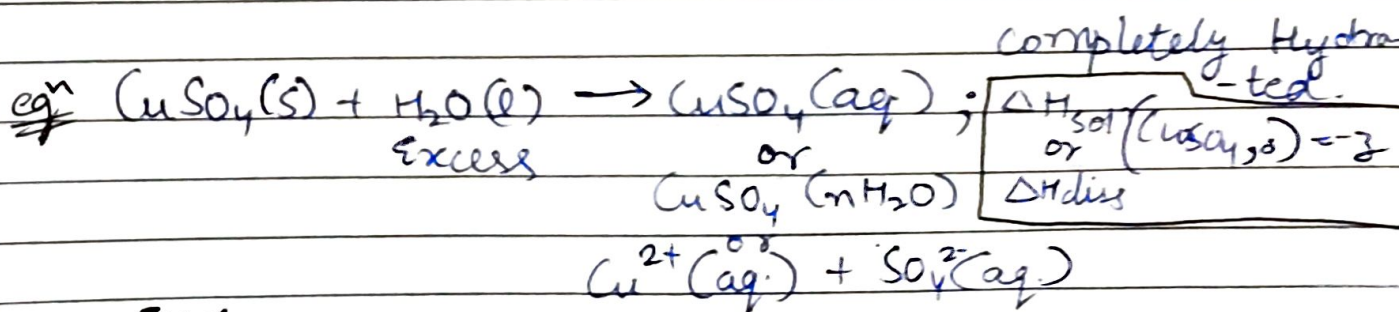


$$\boxed{|x| > |-y|}$$

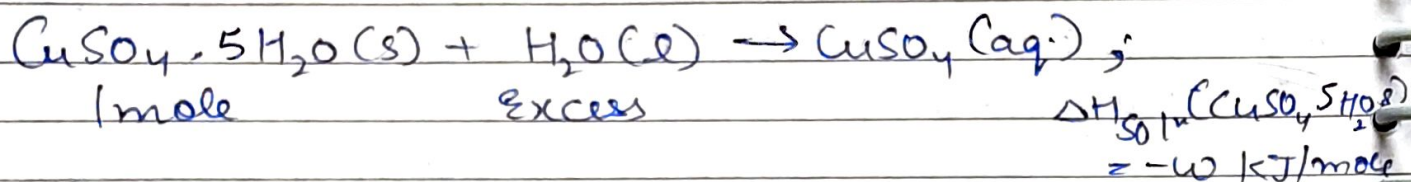
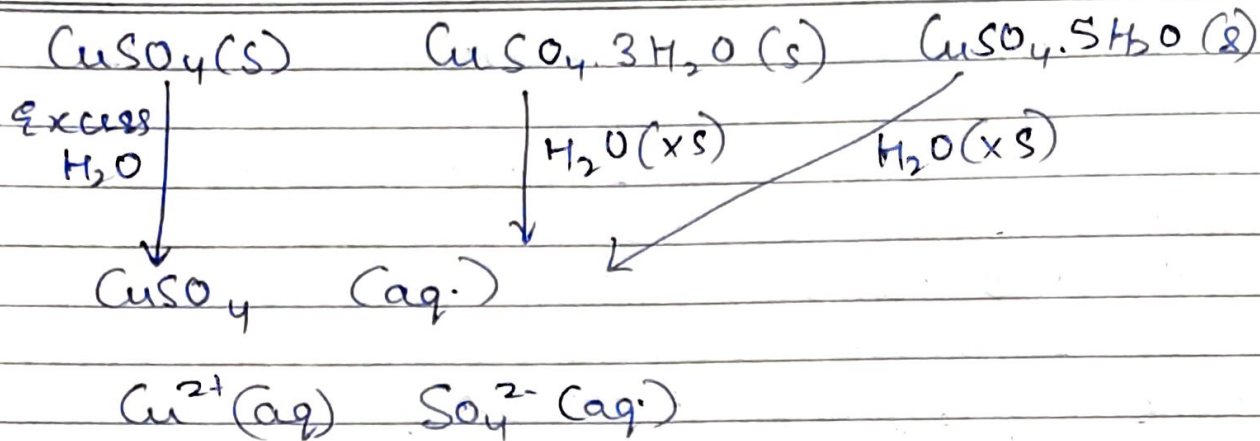
When compound is solid

### (4) Enthalpy of Solution or dissolution

Enthalpy change 1 mole of substance is completely dissolved in excess of solvent. → can be anhydrous, partially Hydrated or



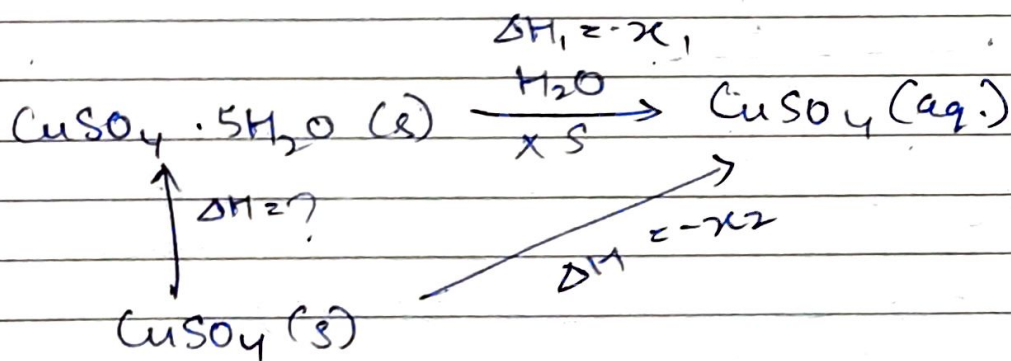




Q  $\rightarrow \Delta H_{\text{soln}}(\text{CuSO}_4 \cdot 5\text{H}_2\text{O}, \text{s}) = -x_1 \text{ kJ/mole}$

$\Delta H_{\text{soln}}(\text{CuSO}_4, \text{s}) = -x_2 \text{ kJ/mole}$

$\Delta H_{\text{hyd}}(\text{CuSO}_4, \text{s}) = ?$



$\Delta H + \Delta H_1 = \Delta H_2$

$\Delta H - x_1 = -x_2$

$\Delta H = x_1 - x_2$

## ★ Spontaneous Process

→ are those process which occur on its own without any constant external support.

→ can be initiated.

→ Irreversible (proceed in one direction)

→ Can be fast or slow

→ e.g. (i) all Natural processes.

(earthquake, rain, increase in Height of mountain)

(ii) Diffusion of Gas

(iii) Mixing of Gas

(iv) waterfall

(v) Burning of Gasoline, petrol, diesel etc

(\*\*) Entropy (S) → State function

→ Extensive property

→ Defined to explain spontaneity of process.

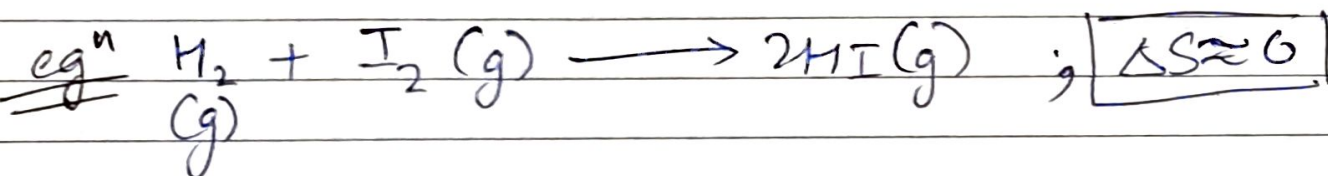
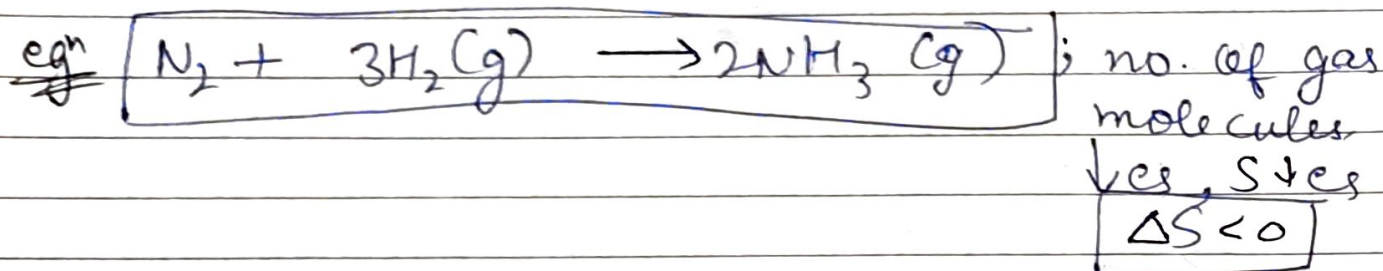
→ It is measure of degree of randomness or disorder or patternless behaviour for maximum dissipation of Energy.



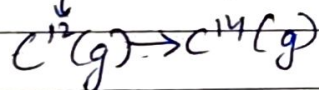
at a given Temp,

$$\Rightarrow S(\text{gas}) \gg S(\text{liq.}) > S(\text{solid})$$

$\Rightarrow$  for a Rx<sup>n</sup> in System, no. of gaseous moles  $\uparrow$ es,  $S \uparrow$ es,  $\Delta S_{\text{system}} > 0$



$\Rightarrow$  for isotopes, more Mass No.  $\rightarrow$  More S



$\Rightarrow$  Crystallization process  $\Rightarrow$  ~~liq.~~  $\rightarrow$  Solid,  $S \downarrow$ es,  $\Delta S < 0$

$\Rightarrow$  Melting of ice  $\Rightarrow$  Solid  $\rightarrow$  liq ;  $S \uparrow$ es,  $\Delta S > 0$

★ Imp

$\Rightarrow$  Boiling of egg  $\Rightarrow S \uparrow$ es,  $\Delta S > 0$

$\rightarrow$  Due to high temp, proteins  $\rightarrow$  Denaturation of Protein  
 molecules Breaks & no. of molecules  $\uparrow$ es, So more randomness.

⇒ Stretching of Rubber / Spring

flexibility lies on stretching, So  $\Delta S < 0$

## # 2<sup>nd</sup> Law of Thermodynamics ÷

Limitation of 1<sup>st</sup> Law → Energy change takes place But direction of change is not defined.

Process  
or  $R \times n$

will move in that direction where Entropy of Universe is continuously increasing

↓  
Sys. + Surroundings

for Spontaneous process or feasible process (Irreversible)

Total Entropy change  $> 0$  ⇒ for non-isolated system  
↓  
Universe

$$\Delta S_{\text{system}} + \Delta S_{\text{surrounding}} > 0$$

$$\Delta S_{\text{universe}} > 0$$

or

$$\Delta S_{\text{Total}} > 0$$

for isolated system

$$\Delta S_{\text{sys}} > 0 \text{ for spontaneity}$$

Spontaneous process proceed in a particular dir<sup>n</sup> until Total Entropy become max. &  $\Delta S_{\text{Universe}} = 0$   
Spiral



# # Reversible $R_x^n$ or Process at Eq<sup>n</sup>

$\Delta S_{\text{universe}} = 0$   $S_{\text{max}}$  for system  
 or  $\Delta S_{\text{Total}}$   
 $\Delta S_{\text{system}} = -\Delta S_{\text{surrounding}}$

## # Non-spontaneous or Non-feasible process

Entropy of universe must be decreasing in non-spont. direc<sup>n</sup>.

constant external support is required

$$\Delta S_{\text{universe}} < 0$$

## # More entropy, more stability of system at given temp.

Mathematically

$$\text{Entropy change } (ds) = \frac{dq}{T}$$

$$\Delta S = \int ds = \int \frac{dq}{T}$$

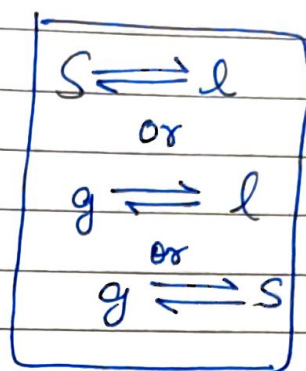
$dq \rightarrow$  Heat exchange b/w system & surrounding

$$\Delta S_{\text{system}} = \int \frac{dq_{\text{system}}}{T}$$

$$\Delta S_{\text{surv.}} = - \int \frac{dq_{\text{system}}}{T}$$

Date .....

# ① Phase Change PROCESS / reaction

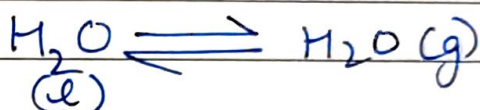


→ occur at given T. and P.

$$q_p = \Delta H$$

$$\Delta S = n \times \frac{\Delta H}{T}$$

Enthalpy of change  
↓  
moles of substance



$$\Delta H_{\text{vap.}} (H_2O, l) = x \text{ KJ/mole at } 100^\circ\text{C}$$

$$\Delta S = \frac{x \text{ J/K}}{373}$$

## ② No Phase Change

$$q = nC\Delta T \quad \text{only temp. changes}$$

$$P = \text{constant}$$

$$\Delta S = \int_T \frac{dq_p}{T}$$

$$\Delta S = \int_{T_1}^{T_2} \frac{nC dt}{T}$$

Ⓒ → Molar Heat capacity  
→ Temp. dependent.



But if Temp. dependency not given, then consider it to be independent of temp.

(\*) If  $C_p$  temp. independent

$$\Delta S = nC \ln \left[ \frac{T_2}{T_1} \right]$$

(3) For ideal gas in system

Changing its condition from

$$P_1, V_1, T_1 \longrightarrow P_2, V_2, T_2$$

$$\Delta S_{\text{sys.}} = \int \frac{dq}{T}$$

$$= \int \frac{dU + PdV}{T}$$

$$\begin{aligned} dq &= dU + PdV \\ dU &= dq - PdV \\ dU &= dq + dw \end{aligned}$$

$$\Delta S_{\text{sys.}} = nC_v \ln \left[ \frac{T_2}{T_1} \right] + nR \ln \left[ \frac{V_2}{V_1} \right]$$

$$\Rightarrow nC_v \ln \left[ \frac{T_2}{T_1} \right] + nR \ln \left[ \frac{P_1}{P_2} \times \frac{T_2}{T_1} \right]$$

$$= nC_v \ln \left[ \frac{T_2}{T_1} \right] + nR \ln \left[ \frac{P_1}{P_2} \right] + nR \ln \left[ \frac{T_2}{T_1} \right]$$

$$\Rightarrow n \ln \left( \frac{T_2}{T_1} \right) (C_v + R) + nR \ln \left( \frac{P_1}{P_2} \right)$$

Also,  $\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$  (Since moles of gas constant)

$$\Delta S_{\text{sys.}} = n C_p \ln \left[ \frac{T_2}{T_1} \right] + nR \ln \frac{P_1}{P_2}$$

### # $\Delta S$ in various Process

① Isothermal Process  $\Rightarrow T_1 = T_2$   $\ln \frac{T_2}{T_1} = 0$

@ Reversible  
Process

Ideal gas

$$\Delta S = nR \ln \left[ \frac{V_2}{V_1} \right] = -2.303 nR \log \left( \frac{V_2}{V_1} \right)$$

or  
 $nR \ln \left( \frac{P_1}{P_2} \right)$

$$\Delta S_{\text{system}} + \Delta S_{\text{surrounding}} = 0$$

$$\Delta S_{\text{sur.}} = -\Delta S_{\text{sys.}}$$

$$= \left[ -nR \ln \left( \frac{V_2}{V_1} \right) \quad \text{or} \quad -nR \ln \left( \frac{P_1}{P_2} \right) \right]$$



(b) Irreversible isothermal process

$$\Delta S_{\text{total}} > 0$$

$$\text{Isothermal} \rightarrow \Delta T = 0$$

$$\Delta U = 0 = nC_V \Delta T$$

$$\Delta H = 0 = nC_P \Delta T$$

$$\Delta S_{\text{system}} + \Delta S_{\text{surrounding}} > 0$$

$$\Delta S_{\text{sys.}} = nR \ln \left( \frac{V_2}{V_1} \right)$$

or

$$nR \ln \left( \frac{P_1}{P_2} \right)$$

$$W_{\text{irr}} + q_{\text{irr}} = \cancel{\Delta U} \rightarrow 0$$

$$-q_{\text{irr}} = W_{\text{irr}}$$

$$\Delta S_{\text{surr.}} = \frac{(-q_{\text{sys.}})_{\text{irr}}}{T}$$

$$\Delta S_{\text{surr.}} = \frac{W_{\text{irr}}}{T}$$

$$\Rightarrow \frac{-P_{\text{ext}} (V_2 - V_1)}{T}$$

$$\Rightarrow -P_{\text{ext}} \left( \frac{nRT}{T} \right) \left( \frac{1}{P_2} - \frac{1}{P_1} \right)$$

$$\Delta S_{\text{surroundings}} = -P_{\text{ext}} \times (nR) \times \left[ \frac{1}{P_2} - \frac{1}{P_1} \right]$$

### # Adiabatic Process

$$q=0 ; \Delta S_{\text{surroundings}} = 0 \rightarrow \text{whether rev or irr.}$$

#### a) Reversible

$$\Delta S_{\text{sys.}} = -\Delta S_{\text{surroundings}}$$

$$\Delta S_{\text{sys.}} = 0 = \Delta S_{\text{surroundings}}$$

#### b) Irreversible

$$\Delta S_{\text{sys.}} > 0$$

$$\Delta S_{\text{surroundings}} = 0$$

### ③ Isochoric $V_1 = V_2$ $nR \ln \frac{V_2}{V_1} = 0$

for Ideal Gas

$$\Delta S = nC_v \ln \left( \frac{T_2}{T_1} \right)$$

### ④ Isoobaric $P_1 = P_2$

$$\Delta S = nC_p \ln \left( \frac{T_2}{T_1} \right)$$



**\*\* Gibbs free Energy ( $G$ )** → state function, Ext property

→ Energy available in the system that can be used to obtain Useful work under const.  $T, P$ .

- non PV work
- magnetic work
- Electrical "
- $Rx^n$

$$(i) \Delta G_{sys} = \Delta H_{sys} - T \Delta S_{sys}$$

$$(ii) \Delta G_{sys} = -T \Delta S_{Total}$$

$$G = H - TS$$

→ Only defined for system

→ very useful Relat<sup>n</sup> ⇒  $dG = VdP - SdT$

only  $T$  const.  $dT = 0$

Isenthal

$$dG = VdP$$

$$dG = \frac{nRT}{P} dP$$

**\*\***  $\left(\frac{dG}{dt}\right)_P = -S$  ( $dP=0$ )

$\left(\frac{dG}{dP}\right)_T = V$  ( $dT=0$ )

$$\Delta G = nRT \ln \left( \frac{P_2}{P_1} \right)$$

$$= nR \ln \left( \frac{V_1}{V_2} \right)$$

→ will remain Spon. till  $S_{Total}$  becomes max. &  $G$  becomes min.

Spon. Process

$$\left[ \begin{array}{l} \Delta S_{Total} > 0 \\ \Delta G_{sys} < 0 \end{array} \right]$$

Rev. Process (at  $eq^n$ )  $\Rightarrow S_{max}, G_{min}$

$$\boxed{\Delta S_{Total} = 0 \quad \Delta G_{sys} = 0}$$

Non Spontaneous

$$\Delta G_{sys} > 0$$

$$\Delta S_{Total} < 0$$

is at

⊕ for Any  $Rx^n$  or Process in system

$$\Delta G_{sys} = \Delta H_{sys} - T \Delta S_{sys}$$

$$\Delta G_{sys}$$

$$\Delta H_{sys}$$

$$\Delta S_{sys}$$

i) Always -ve  
(spontaneous  
at any temp.)

-ve (exo)

+ve

(ii) Always +ve  
(non Spont.  
always)

+ve

-ve

(iii)  $|\Delta H| > |T \Delta S|$   
at low Temp.  
 $\Delta G = -ve$ , Spont.

-ve

-ve

$|\Delta H| < |T \Delta S|$   
at High Temp.

$\Delta G = +ve$ , Non-spont.  
Spiral



(iv) <u>Spont.</u> at High Temp. → $\Delta G = -ve$	$\Delta H_{sys.}$ +ve	Date ..... $\Delta S_{sys.}$ +ve
<u>non-sp.</u> at low Temp. → $\Delta G = +ve$		

**\*\* Graphite → Diamond**

G → D ;  $\Delta H = +ve$  (endo)  
ordered  $\Delta S = -ve$   
 $\Delta G = +ve$  (always)

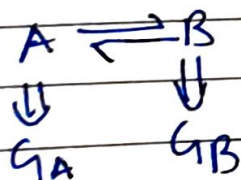
$$\begin{array}{|c|} \hline \Delta H = -ve \\ \Delta S = -ve \\ \hline \end{array} \rightarrow \Delta G = \Delta H - T(\Delta S)$$

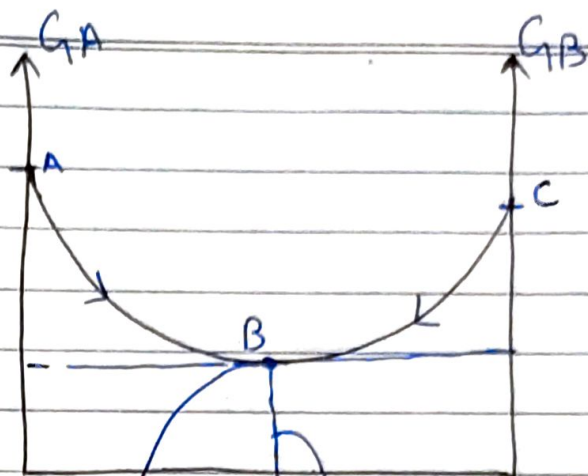
$\downarrow$        $\downarrow$        $\downarrow$   
 -ve      -ve      +ve

**#** Temp. at which  $Rx^n$  or Process Achieves Eq<sup>n</sup>  
 $\Delta G = 0 = \Delta H - T\Delta S$  usually Phase change

$$T = \frac{\Delta H}{\Delta S}$$

**#** Rev.  $Rx^n$  → always achieves Eq<sup>n</sup>



 $G_{min}$ Eq<sup>n</sup> point $\Delta G = 0$ 

Progress of  
Rxn w.r.t  
time

Sp. (Irr.)

$$\Delta S_{univ.} > 0$$

$$\Delta G_{sys} < 0$$

Rev  $\Rightarrow$  Eq<sup>n</sup>

(S<sub>max</sub>)<sub>univ.</sub>  
 $G_{min}$

$$\Delta S_{sys.} = \frac{\Delta H}{T}$$

$$\Delta H_{sys.} - T \Delta S_{sys.} = \Delta G = 0$$

$$\Delta S_{Total} = 0$$

#  $G = H - TS$

at const. T, P

$$\Delta G_{sys.} = \Delta H_{sys.} - T \Delta S_{sys.}$$

#  $dG = VdP - SdT$

$$G = f(T, P)$$



Date .....

only T. const.

$$\boxed{dG = VdP}$$

$$\left(\frac{\partial G}{\partial P}\right)_T = V$$

for Ideal Gas

$$dG = nRT \frac{dP}{P}$$

$$\Delta G = \int dG = nRT \int \frac{dP}{P}$$

$$\boxed{\Delta G = nRT \ln \frac{P_2}{P_1}}$$

Const. P only

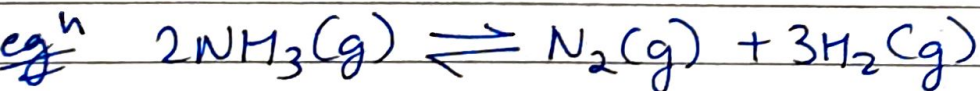
$$dG = -SdT$$

$$\boxed{\left(\frac{\partial G}{\partial T}\right)_P = -S}$$

⊕ Rev.  $R \times^n$



$$K_{eq} = K_c^n \text{ const.} = \frac{[B]^b}{[A]^a}$$



$$K_{eq} = \frac{[N_2]^1 [H_2]^3}{[NH_3]^2}$$

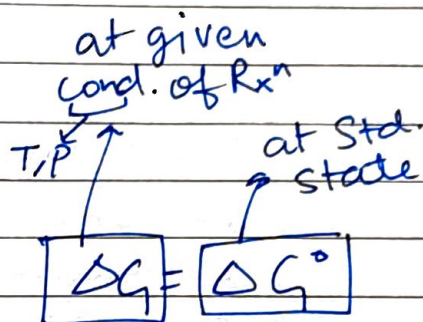
$[N_2]$  = molarity of  $N_2$

$$= \frac{n_{N_2}}{V}$$

Vol. of container

# At Non-Eq<sup>n</sup> point  $\Rightarrow$  Free Energy is still available  
 $\Delta G \neq 0$

$\Rightarrow$  Conc Ratio  $\neq K_{eq}$



$\Rightarrow$  Conc Ratio = Reaction Quotient (Q)

At Eq<sup>n</sup>  $\Rightarrow \Delta G = 0$ ,  $G_{min}$

$\Delta G^\circ \rightarrow$  may or may not be zero

$$Q = K_{eq}$$

$$0 = \Delta G^\circ + RT \ln(K_{eq})$$

$$\frac{-\Delta G^\circ}{RT} = \ln(K_{eq})$$

$$\frac{-\Delta G^\circ}{RT} = 2.303 \log(K_{eq})$$

$$(K_{eq} = e^{\frac{-\Delta G^\circ}{RT}})$$

$$K_{eq} = 10^{\left(\frac{-\Delta G^\circ}{2.303 RT}\right)}$$

or

$$K_{eq} = \text{anti log} \left( \frac{-\Delta G^\circ}{2.303 RT} \right)$$



# \*\*\* Third law of Thermodynamics

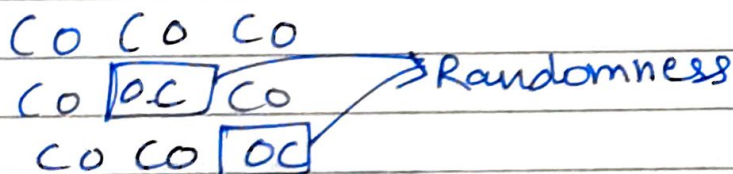
At 0K (Absolute zero) Entropy of perfectly crystalline substance is zero.

$$S_{0 \text{ kelvin}} = 0$$

Exception :-  $\text{Cl}_2$  (Solid)  
CO (Solid)  
NO (Solid)  
H<sub>2</sub>O (Solid)  
H<sub>2</sub> (Solid)  $\rightarrow S_{0K} \neq 0$

there must be some residual entropy due to random arrangement

due to existence of ortho & para form



# Due to 3<sup>rd</sup> law, Absolute value of entropy can be obtained provided molar Heat Capacity is temp. dependent.

Solid Sub (A)  $\longrightarrow$  Solid Subst. (A)  
0K T K

$$\Delta S = \int_{S(0K)}^{S(TK)} dS = n \int_{T_1=0K}^{T_2=TK} \frac{C_p dT}{T}$$

C can be like  $aT^2 + bT$

$$S_{TK} - S_{OK} = n \int_{T_1}^{T_2} \frac{cdT}{T}$$

### ⊕ Zeroth law of Thermo

If Body A & B are in thermal Eq<sup>n</sup>, B & C are in thermal Eq<sup>n</sup>, then A & C must be in thermal Eq<sup>n</sup>.

$$T_A = T_B$$

$$T_B = T_C$$

then  $T_A = T_C$